

# **The Sweetest Lesson**

**Your Brain Versus AI**

David Spuler

Aussie AI Labs

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# About the Author

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Other than writing, he's an avid AI researcher with a Ph.D. in Computer Science and decades of professional experience. Most recently, Dr. Spuler has been founding startups, including the current Aussie AI startup and multiple high-traffic website platforms with millions of monthly uniques, including an e-health startup acquired by HealthGrades, Inc. Prior roles in the corporate world have been as a software industry executive at BMC Software, M&A advisor, strategy consultant, patent expert, and prolific C++ coder with expertise in autonomous agents, compiler construction, internationalization, ontologies and AI/ML. Contact by email to [research@aussieai.com](mailto:research@aussieai.com) or connect via LinkedIn.

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# Preface

*“I would like to die on Mars.*

*Just not on impact.”*

— Elon Musk.

## **Why a Book on The Sweetest Lesson?**

Who doesn't like the sweet taste of success? Let's celebrate the powers that make humans special by comparing ourselves to the latest technological advances in an AI world. There's far too much hype in this world about AI, and not enough hype about the amazing capabilities of the carbon-based bio-robots, otherwise known as people.

## **How This Book is Organized**

The best way to read this book is to open all the pages and then read them all at the same time. That's how an AI model would do it on their parallelized NVIDIA GPU chips, and what's good enough for silicon should work in carbon.

Alas, no.

Sadly, the book is organized sequentially, because we are logical lifeforms and we've been trained to read one page at a time. Oddly, our brains can process a huge volume of input signals in parallel, so maybe we could read all the pages in parallel, if only we were to try!

## About Aussie AI

Aussie AI is a platform for the development of consumer AI applications, with a special focus on AI-based writing and editing tools for fiction. Our premier applications offer an extensive range of reports and error checks for both fiction and non-fiction writing, from a full-length novel to a short report. Please try it out and let us know what you think: <https://www.aussieai.com>

## Our AI Research

The primary focus of research at Aussie AI is on optimizing LLM inference algorithms (i.e., “running” the model after training or fine-tuning), and our research is toward the following aims:

- Fast on-device model inference, specifically for smartphones and AI PCs.
- Scaling inference algorithms to large volumes of requests.
- Efficient GPU inference algorithms (hardware acceleration).
- Non-GPU inference optimization algorithms (i.e., software methods).

## Disclosure: Minimal AI Authorship

Despite my being involved in the AI industry, there was almost no AI engine usage in creating this book's text or its coding examples. Some text has been analyzed and reviewed using Aussie AI's editing tools, but not even one paragraph was auto-created by any generative AI engine. All of the code is also human-written, without involvement of any AI coding copilot tools. I mean, who needs them?

However, AI was used in several ways. AI-assisted search tools were very useful in brainstorming topics and researching some of the technical issues. The main cover art image was AI-generated by Google ImageFX, followed by human editing.

## Disclaimers

Although I hope the information is useful to you, neither the content nor code in this work is guaranteed for any particular purpose. Nothing herein is intended to be personal, medical, financial or legal advice. You should make your own enquiries to confirm the appropriateness to your situation of any information.

Many code examples are simplistic and have been included for explanatory or educational benefit, and are therefore lacking in terms of correctness, quality, functionality, or reliability. For example, some of the examples are not good at handling the special floating-point values such as negative zero, NaN, or Inf.

Oh, and sometimes I'm being sarcastic, or making a joke, but it's hard to know when, because there's also a saying that "Truth is often said in jest!" Your AI engine certainly won't be able to help you sort out that conundrum.

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I hope you enjoy the book! Please consider leaving a review on the website where you purchased the book. Since few readers do this, each review is important to me, and I read them all personally.

### **Feedback and Contacts**

Feedback from readers is welcome. Please feel free to tell us what you think of the book, the research literature review, or our Aussie AI software. Contact us by email via [support@aussieai.com](mailto:support@aussieai.com).





# Table of Contents

About the Author.....	3
About the Contributors.....	4
Preface.....	5
Table of Contents.....	9
<b>1. Your Brain Versus AI .....</b>	<b>15</b>
Your Brain is Bigger .....	15
Your Brain is More Efficient .....	17
Your Brain Learns Like AI.....	18
References .....	19
<b>2. The Bitter Lesson.....</b>	<b>21</b>
What is The Bitter Lesson? .....	21
Bitter Chess.....	23
Intelligence and the Bitter Lesson.....	24
References .....	25
<b>3. Intelligence.....</b>	<b>27</b>
Unintelligent AI.....	27
Similarities .....	28
Differences.....	29
AI Thinking Limitations .....	29
Weird Problems.....	30
Specific Thought Problems .....	31
Solved Problems.....	32
References on AI Intelligence.....	33

**4. Weak Words .....37**

Words and Dumbness .....37

Strawberries .....38

Illegal Chess Moves .....39

Bad Names.....40

Over-Alignment .....41

3D Worldview .....42

Catastrophic Forgetting .....42

Slowness .....43

References .....44

**5. Neurology Versus Numbers .....47**

Neurology versus Numbers .....47

Activated Brain Regions .....48

AI Copies of Brain Regions .....49

Studying AI Model Numbers.....50

The 10% Rule.....51

Neurosurgery on AI Brains .....52

References .....53

**6. Fast & Slow Thinking.....59**

Fast and Slow Systems .....59

How Much Faster? .....60

Fast Thinking.....61

Slow Thinking .....62

How Does AI Think?.....63

Controller Mechanism .....64

Fast Versus Slow Reasoning .....64

Hierarchical Reasoning Models .....65

Subliminal Learning.....66

References.....67

<b>7. The Wall</b>	<b>71</b>
Remember The Wall?	71
Wall Obliterated	73
References on the AI Wall	74
<b>8. Data Crisis</b>	<b>77</b>
Training Data Sizes	77
Data Shortage	78
Synthetic Data	78
Model Collapse	79
People Parrots	80
References	81
<b>9. Reasoning Models</b>	<b>85</b>
Reasoning Prompts	85
Chain-of-Thought	86
Emotional Prompting	87
Skeleton-of-Thought Prompting	87
Two-Step Reasoning	88
Multi-Step Reasoning	89
Deep Research Models	90
Meta-Reasoning	90
Not Following Instructions	92
RAG Reasoning	93
Implicit Associative Priors	93
Really Radical Reasoning References	95
<b>10. Concepts</b>	<b>105</b>
What are Concepts?	105
Large Concept Models	107
References	108

**11. Reading & Writing .....115**

AI Reading and Writing..... 115

Prefill for Reading..... 117

Decoding for Writing..... 118

Reading Limitations..... 119

References ..... 120

**12. 'Rithmetic..... 129**

Everyone Loves Math..... 129

Symbolic Execution..... 131

References ..... 133

**13. Tools ..... 139**

What are Tools? ..... 139

Integration of Tools ..... 141

Computers as Tools..... 142

LLM Hooks ..... 143

References ..... 143

**14. Brainy Body ..... 149**

Brain Versus Brawn..... 149

Why Embodied? ..... 151

Fake Versus Real Bodies..... 152

References ..... 153

**15. Faster AI ..... 155**

Faster AI..... 155

Endless Matrix Multiplications ..... 156

500 Ways to Optimize..... 156

Training ..... 159

Don't Forget the Network ..... 160

The Question..... 161

References ..... 162

**16. The Sweetest Lesson ..... 163**

    Brains are 50 Times Bigger.....163

    Really That Big?.....165

    Maybe Less.....165

    Maybe More.....166

    Smart Coding.....167

    The Bitter Lesson Again .....167

    The Sweetest Lesson .....168

    References .....169



# 1. Your Brain Versus AI

*“You are more powerful than you think.”*

— Tim Cook.

## Your Brain is Bigger

Your brain is big and it’s definitely a lot bigger than any AI engine. If you talk to an AI chatterbox for a while, you’ll probably start to realize that it’s not actually as intelligent as it should be, and here’s the main reason: it’s not big enough.

The human brain is so large that it’s difficult to quantify it with an exact number, but the prevailing theory is that you have around 100 trillion synapses that connect about 86 billion neurons. We’ll examine the evidence for those numbers in a later chapter, but for now, note that there are therefore more than 1,000 synapse connections per neuron, although some estimates are as high as 7,000 for the ratio, which would mean 700 trillion human synapses. A trillion is a one followed by 12 zeros, so these numbers are not small. You can’t count that many synapses with a microscope and a hand-clicker, but feel free to try.

AI engines vary in size, but none are anywhere near that big. Instead of 86 billion neurons, they usually have a “model size” or “hidden dimension” of about 7,268. That’s about 11 million times smaller, if you wanted an ego boost.

The equivalent of a human synapse in an AI model is called a “weight” and it’s just one number. Like synapses, these weights can either intensify or reduce a “signal” in the silicon brain, depending on whether they’re large numbers or small fractions.

All AI engines are smaller in size than the human brain. OpenAI’s GPT-4 was reportedly about 1.76 trillion weights, or let’s say 2 trillion to be kind, which is still 50 times smaller than 100 trillion carbon-based synapses.

Also, GPT-4 really only used 200 billion weights at a time in what’s called a “Mixture-of-Experts” architecture, which is abbreviated as “MoE” (to remember this, think of *Moe’s Tavern* in *The Simpsons*, which probably has a few “experts”). So, that’s 500 times smaller than a brain, if you’re keeping count.

But GPT-4 is over a year old and not state-of-the-art as I write this. Not all of the top frontier models disclose their sizes, but I can tell you a few. The Google Gemini 1.5 Pro was about one trillion weights (100 times smaller).

The DeepSeek R1 model, which caused a huge flutter in the industry when released, had multiple models ranging in size up to 671 billion weights, about a quarter the size of GPT-4, so that’s 200 times smaller. DeepSeek R1 also used the “MoE” architecture, at 37 billion weights per invocation, which is 2,700 times smaller.

The latest one this week as I write this, and these leaderboards seem to change every week, is the Kimi K2 model from Moonshot AI, which has around 1 trillion weights (100 times smaller) with a 32B MoE architecture (3,125 times smaller than a brain).

You can pick any of these numbers that make you feel good, even up to the fun fact that AI has 11 million times fewer neurons. That’s probably wishful thinking and it also seems unfair to compare our total synapse counts against the smaller “MoE” subsets of activated weights in those models, rather than their full weight counts. Humans also don’t “activate” all of their brain, or haven’t you seen any of the Hollywood movies with this premise?

So, let’s compare human synapses to AI weights. Personally, I think the most likely number is close to this: based on 100 trillion synapses versus two trillion weights, you are at least 50 times smarter than an AI engine.



# Your Brain is More Efficient

Despite being massively bigger, your brain is far more energy-efficient to run. The typical comparison is that your brain is like a 20 watt lightbulb, except that nobody ever turns it off, because you need it to keep breathing. Inside your head, you're always "burning the midnight oil" even while you sleep. For comparison, a single high-end GPU chip in a data center uses hundreds of watts.

Your brain actually runs hotter than most other animal species. The brain consumes 20% of the human body's total energy output (100W), despite only being 2% of our body weight.

You've probably heard that the advancement of human intelligence was spurred along by one of these theories:

1. Our ability to stand upright.
2. A larger brain space in the skull (also somewhat related: being taller).
3. The invention of fire to allow cooking to expose enough nutrients to feed our brain.

But there's another one that gets less attention:

*The invention of sweating.*

Our brain runs so hot that we would overheat without sweating, because even 20 watts is quite a heatload in an enclosed space. Exposed skin with sweat glands is critical to evaporate sweat, and this "evaporative cooling" is what makes sweating work. Most other animal species can't sweat enough to radiate enough heat away. Hence, evolutionary brain size was limited by the inability to sweat.

In order to sweat, we needed to lose most of our hair, too. Animal fur interferes with sweating in most species, which is why your pet dog hangs its tongue out the car window all the time, although maybe it's also fun. Hence, if you're balding in your old age, you can now say it's a sign of high intelligence.

All of those AI GPU chips need "liquid cooling" to run hot, too. It runs in pipes under "raised floors" inside massive data centers. That's another way that your brain is better than AI: your brain uses a lot less water, also.

# Your Brain Learns Like AI

No, that's wrong. Your brain is not like AI, because your intelligence came first, and the AIs are a recent invention. AI is like your brain, because it was designed by scientists to use the same brain-like methods.

AI is a copy.

The idea is called a “neural network” and yours uses chemicals and carbon-based molecules, whereas AI uses GPU chips that run on electricity in silicon.

Your brain learns like AI, because the “training” of LLMs is based on your neural network. In the brain, the mappings between neurons are adjusted via “synaptic plasticity,” which doesn't mean they're made of plastic, but that they are soft and changeable.

AI mappings are numbers called “weights” and they are changed by adding or subtracting small amounts to these numbers, as the LLM training process scans through reams and reams of pre-written text.

The technical term for how AI models get better weights is “backpropagation” because the “forward pass” reads the data, and then the “backward pass” propagates small changes to the weights, so that they'll be better next time. This is a slow process, sometimes even taking weeks or months for a big model, modifying the LLM weights a tiny amount each document they read.

They say that humans need 10,000 hours of practice to master a task. Well, AI engines need a lot more than 10,000 GPU hours of computation for their weights to converge to numbers that make it smart.

Hence, another point: your brain learns faster than AI.

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## 2. The Bitter Lesson

*“AI is a marathon, not a sprint.”*

— Demis Hassabis.

### What is The Bitter Lesson?

Although the previous sections should have you on a high about your amazing brain, this is where we have to take a long, hard look at the history of analyses like that in the computer industry. It’s very bitter.

The idea of the “bitter lesson” was coined in 2019 by Rich Sutton in relation to intelligent computing. The core of the idea is that a simple algorithm combined with brute-force computer power will always eventually outperform apparently smarter algorithms.

The reason that this idea is “bitter” is that human researchers tend to assume that making computers more like them, by using tricky human-like rules of thumb (called “heuristics” by boffins), will be the best way.

It usually works for a while, but then there’s the reality that these advanced research algorithms get overrun by much simpler and dumber algorithms, without any fancy logic, hooked up to a very fast computer.

When presented with a new problem, human researchers will try to solve it like humans. Hence, they will use things based on human-like intelligence, such as:

1. Heuristics
2. Logic

Heuristics are human-like “tricks” or “shortcuts” in solving a problem that are then coded up into a computer algorithm. Logic is part of this, where possible solutions are analyzed according to some rational metrics. So, this is the general approach:

How do we find some of the possible solutions? — Heuristics.

What’s the best solution? — Logic.

These types of methods often do well in the short-term in solving a problem, even on fast computers at the time. However, over time, computers get even faster, and the best algorithms often turn out to involve:

1. Brute-force computations, and
2. Very simple comparisons.

It’s kind of like that movie *Everything Everywhere All at Once*, only not quite as funny.

You don’t need heuristics to find the best solution. Instead, just get a faster computer and *try all of them*. The general approach changes to:

How do we find the possible solutions? — Try every single one.

What’s the best solution? — Compare them all.

When this solves a problem better than the early heuristic versions, it’s a “bitter lesson” for the initial human researchers. And I mean, at a level of bad taste in the mouth beyond what you get from a dandelion sandwich. Researchers think the solution should be something clever, but there’s nothing smart about this brute-force approach, and it’s just a dumb box cranking through the whole solution space. It shouldn’t work so well, but it does.

Bitterness ensues. Lots of musty research papers get torn up by librarians and tossed in the trash.

It's happened in the computer industry, over and over again, and yet when researchers are presented with a new problem to solve, they still tend to try heuristics and logic.

Why is it so hard to learn from these mistakes, rather than learn that raw compute always wins? Maybe, it's because of what it implies at the deepest levels of the soul:

*Computers are better than humans.*

Surely, it can't be true?

## Bitter Chess

Chess-playing computers are the best example of the bitter lesson. The best chess computer in the world is named Stockfish, and it has a rating of over 3,000 ELO points. The best grandmasters are “only” around 2,700 points on this rating scale.

The way it started was that programmers tried to copy how humans play chess. There are also sorts of rules of thumb that you learn at Chess Club, such as:

- Center your pieces.
- Queens are worth nine pawns.
- Make a breathing space for your king.

A computer can play a reasonably strong game of chess if you code up these sorts of rules. It's rating is maybe around 1,600 if you do this. My favorite reference on this is the 1988 book by David Levy.

The first major improvement came shortly after. If you combine these rules with a very powerful computer that scans through lots of possible moves, it does better. Not smarter rules, but just more grunt to scan all the whole tree of possible moves that each player can make. This was IBM's “Deep Blue” computer that played chess, and it was about the level of the World Chess Champion at the time, Garry Kasparov, who beat Deep Blue in the first match in 1996, but lost the rematch a year later.

Not smarter, just faster, but still using human techniques. Half bitter.

What followed was even worse. It turns out that computers don't even need the human rules of thumb. In 2017, an AI company called DeepMind created an even more massive computer called AlphaZero, that was better at chess. This would be fine, except for the way that it did so.

All of those rules of thumb about how to play chess well, crafted by humans over centuries of careful analysis: *worthless*. AlphaZero only needed the basic rules of chess and a lot of GPU chips to run the AI learning algorithm. Rather than requiring software code for these heuristic rules of thumb, AlphaZero just played lots of random games against itself, watching for what works, and what doesn't. The computer played better just by figuring out what to do itself, learning all of the types of patterns in the game, using methods that humans cannot even understand.

Now that's bitter.

## Intelligence and the Bitter Lesson

Will the achievement of human-level intelligence be another case of the bitter lesson? If the best models are at 2 trillion weights and the human brain has about 100 trillion, maybe the problem is just how to brute-force the AI engines with 50 times more power. Is the failure to reach true intelligence just that technology companies haven't yet figured out how to run 100 trillion weights so as to match the true size of the human neural network?

Reasoning could be another bitter lesson. After all, the big kerfuffle around DeepSeek in early 2025 was mainly that reasoning could be done just with training. If you showed the LLM enough mathematical proofs in training, it got better at proving things.

If the AI companies put their minds to it, they'll find training examples for every type of reasoning. Proof by mathematical induction, by contradiction, by algebraic transformations? It's all be done a thousand times in all the research papers. But those are just proofs, and that's just one way to do reasoning.

Are there really that many ways to do reasoning?

And if we crank up our 100 trillion weights in an ultra-massive AI model, and show it all those different examples of reasoning, maybe that's job done. The AI engine has then seen countless examples of the hundreds or thousands of different ways to do reasoning, and it's great at parroting them. Generalization, who needs it?

Is truly intelligent AI going to be the bitter lesson, all over again, one last time?



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# 3. Intelligence

*“Software is eating the world,*

*but AI is going to eat software.”*

—Jensen Huang, May 2017.

## Unintelligent AI

The big goal in AI research is called “Artificial General Intelligence” or “AGI” for short. This refers to having an AI engine that is smart enough to match the general level of human intelligence. Estimates vary as to how many years it will take before we get to AGI in the future. But they all agree on one thing:

*We’re not there yet.*

Sometimes, it seems like we are already at that level. The AIs are so great at mimicking human-like text, that it often feels to us like we’re talking to a real human. But this is human nature to “project” ourselves onto a non-human algorithm. In reality, an AI model has these properties:

- LLMs have no “feelings” or “empathy” (it’s just fake words).
- LLMs don’t “care” if they make mistakes (even when you point them out!).

Your AI buddy doesn't have real feelings for you, but can certainly write words that make it seem that way, because that's how it's been trained. This type of training is called "alignment" or "conversational AI."

An LLM also feels no real "embarrassment" if you point out its mistakes, although, again, it has been trained to handle this type of input situation by saying words like "oops" or "sorry" or whatever. Your challenge to an AI engine about its answer feels not different to it than any other input prompt because, well, it feels nothing either way.

Also, it doesn't matter if you say "please" and "thank you" to an AI engine. Lots of people do, but it's just extra words to the LLM.

It's a machine, and there's literally no feelings anywhere. AI engines really are an "alien intelligence" and not very much like us.

## Similarities

How are brains and LLMs similar? At a high level, there is a great deal of functional and structural similarity in how they perform tasks:

- Fast thinking and slow thinking modes
- Great at pattern recognition
- Nobody understands how they work!

A lot of the limitations of LLMs read like they were written about humans:

- Bad at arithmetic and math (without help from a calculator).
- Have biases, toxicity, and other unwelcome aspects.
- Can't do crossword puzzles well (especially cryptics!).
- Don't like anagrams and word scrambles.
- Forget stuff they were told earlier.
- Need training to be able to work with Windows.

It's like an endless series of memes. LLMs are so much like us!

# Differences

Sure, one is carbon-based and one is silicon. Other than that, they're the same? Well, no, there are other distinctions between your brain and AI.

Differences appear more in the broader structure of the usage of a brain versus an LLM, whereas the low-level structure is a neural network for both.

How are they different in this higher-level functioning? Here's some of the areas for distinction between you and an LLM:

- LLMs are more specialized (e.g., at writing).
- Fast LLMs can process vast reams of information.
- LLMs are integrated digitally to other systems.
- Brains have a human body attached.

You might think it an advantage to have a calculator attached rather than a big glob of pulsating cells, but there's a whole research area that says that AIs won't achieve human-level intelligence without having a body attached. It's called "embodied AI" and predicts that AIs will need to learn about 3D environments by exploring them physically, while being trained with that information.

But, if you want to know the main difference between LLMs and human brains: *dumber than us*. They can perform some impressive brute-force calculations, and are great at writing documents or creating images, but they also make some simple mistakes.

## AI Thinking Limitations

There's a long list of AI limitations, including some I mentioned above, but let's focus on things that humans can do, which LLMs cannot. Despite all the PR hype, the AIs are not that great at:

- Thinking generally ("generalization")
- Conceptual thinking
- Learning on-the-fly
- Continual, incremental learning

Humans can do this stuff in their sleep, literally. Children are just sponges absorbing information.

To understand how poor LLMs are at learning, consider a recent study at Apple by Shojae et. al. (June 2025). They asked some of the best frontier models to solve some abstract puzzles and got some human-like results: as the puzzles got harder, the LLMs failed more. This is actually worse than it sounds, because they failed because they weren't using very general reasoning methods, but mostly relying on pattern recognition.

Let's give them the benefit of the doubt. We'll call it a tie.

Anyway, here's the real kicker: the folks at Apple also did another test where they told the AI exactly how to solve the puzzle. They put the answer to the puzzle in the questions, with detailed instructions on how it can be solved. All the AI needed to do was read the answer, follow the instructions on how to solve the puzzle, and they'd be done.

*It made no difference.*

The LLMs were completely unable to use the answer to help solve the puzzle. They just couldn't map it to their thought pattern, and were completely unable to learn. Zero on-the-fly learning capability. Were they just being stubborn?

I mean, there are humans that don't read the instructions when building flat-packed furniture, and others who won't ask the grocery store clerk where to find the *I Can't Believe It's Not Butter* on the reach-in cooler shelves. But I think anyone else would be happy to take the answer in front of them and use it to solve a complex question. Teachers who put the answers in every question on their surprise math quiz would be immensely popular with their students, although perhaps less so with the School Board.

## Weird Problems

There are some very weird things going on inside the brain of your average LLM. Here are some of the things you might see:

- Making stuff up that looks plausible but is false ("hallucinations" or "confabulations").
- Repeating the same things again that it already told you.
- Never saying it's run out of ideas.
- Never answering "I don't know" ever, ever, ever.

It's like a good friend who can't ever admit they're wrong. They make up stuff rather than backing down in an argument. But even in that case, your human friend is better than the LLM, because the AI:

*Doesn't know it's lying.*

In fact, it has no feelings about it at all. The LLM is just doing its best to spit out the words that look the most like a good answer. You can even challenge it, in which case, it can even spot its own mistakes, and it isn't even embarrassed by this.

I mean, it might be trained to output a few sheepish words when a mistake is found, but it doesn't really know what that means either. It's all just meaningless sequences of words.

## Specific Thought Problems

The above issues are very deep and general aspects of thinking, and what thinking even means. Going deeper, there are specific types of thinking that LLMs are poor at:

- Common sense
- Empathy (the real kind, not the smarmy parroting)
- Understanding the “human condition”
- Senses, textures, touch.
- 2D spatial understanding
- 3D environment understanding
- Large search spaces (e.g., chess games)

Common sense is about a thousand little things. For example, there was a cyclone coming toward my hometown recently, so I asked an AI about what the update was. It came back with a news report from about two years ago, and pleasantly summarized it as an update for me.

That's not common sense.

If you know what a cyclone is, then you understand that I want recent information only. It's like if I ask for the Super Bowl score, I don't want one from 1957. In this case, I think you'll find that the AI gets it correct for the Super Bowl, because this is a fixable problem. It's been trained a lot on Super Bowls, and what various questions people ask, and hasn't been trained much about cyclones, because there are “hurricanes” in the Northern Hemisphere rather than the “cyclones” in Australia (they spin in opposite directions).

I was going to put “reasoning” on that list of things AI is poor at, but maybe it’s no longer very true. It’s still partially true because LLMs are still bad at “temporal reasoning” about time and cause-and-effect, and also “spatial reasoning” in 2D or 3D environments.

However, they’re now amazing at mathematical proofs and other scientific reasoning, not to mention they got better at word puzzles and other meta-cognition about language. There has been an immense amount of research done into “reasoning models” starting with the OpenAI o1 “Strawberry” release in September, 2024.

So, the AI industry is moving fast, and some of the limitations can switch to being solved problems.

## Solved Problems

Some of the capabilities that are not being mentioned as limitations in AI outputs anymore:

- Basic grammar and punctuation
- Instruction following
- Conversational capabilities
- Foreign language outputs

Some of the more technical capabilities include:

- Image file formats (e.g., JPEG).
- Output formatting correctness (e.g., tables or HTML).
- Encoding problems (e.g., emojis in UTF8 versus Unicode)
- Programming language outputs (e.g., Python or C++).
- Processing columns of numbers (like Excel).

Meta-cognition problems in AI that are largely solved:

- Tone of writing (e.g., optimistic versus negative, casual versus formal).
- Style of writing (whatever that may mean).
- Knowing when to stop (e.g., using “stop tokens”).
- Following meta-requests about outputs (e.g., word counts, paragraph lengths, etc.).

The list of solved problems is getting longer with every major release.



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## 4. Weak Words

*“Stitching Together Sequences of Linguistic Forms...*

*Without Any Reference To Meaning:*

*A Stochastic Parrot.”*

— Bender et al., 2021.

### Words and Dumbness

AI models work mainly on words, and therein lies the rub. It’s really tough to do some things using only words. Yes, you can write some exciting poetry in word patterns, but there are problems with:

- Numbers and arithmetic
- Real-life meanings of words
- Common sense
- 3D world modeling
- Time modeling (“cause and effect”)

Words have meaning beyond their basic wordliness, and that’s where the LLM has problems. Words are not good at representing common sense issues.

Common sense are things that we know immediately and take for granted. Here are some common sense ideas:

- Feathers are lighter than stones and fall slower.
- Moving a glass of water differs from moving a drop of water.

Unfortunately, an LLM these things are just words, and that's all they know.

## Strawberries

If LLMs just look at words, why are they terrible at solving crosswords? There were also difficulties with word scrambles or anagrams, and asking for a list of words that start with a particular letter.

A lot of these problematic areas have gotten better recently, but LLMs were initially awful at them.

Even some basic tasks that seemed to be like spelling a word were problematic for early LLMs. The most famous example is:

*How many letter r's in "Strawberry"?*

ChatGPT used to get this wrong, confidently stating that there are two. Is the extra one hidden behind the 't'?

It's not really clear why ChatGPT answered this incorrectly, but this error spawned the codename "Project Strawberry" for the more advanced "reasoning model" from OpenAI named "GPT-4o" that was released in late 2024.

Weirdly, the problem is words.

Counting letters in a word is not really a problem you can solve with words. In fact, it's a "meta-problem" at a level higher than just outputting words. Hence, basic LLMs that think only in words could not perform detailed reasoning about the properties of words, and required extra steps in reasoning models to do so correctly.

# Illegal Chess Moves

I tried to play a game of chess against ChatGPT the other day. My opponent was very keen and quite helpful, chattering along with every move. The game went:

1. e4 e5

2. Nf3 Nc6

3. Bc4 Bc5

4. c3 Nf6

5. b4 Bxb4

At this point, the game ended. ChatGPT complimented me on playing the Evans Gambit with the “b4” pawn move, which is apparently an interesting and enterprising type of chess opening. When I tried to respond with my next move, “6. c3xb4” taking the Bishop, I was informed that it was an illegal move.

I guess we can call it a draw.

Sorry, that’s an inside joke only for chess players. Suffice it to say that ChatGPT was making some very basic mistakes:

1. I didn’t play the Evans Gambit.

2. The ChatGPT move “Bxb4” is terrible (needlessly losing the Bishop).

3. The move I want to play is not illegal.

What’s going on here?

The problem is words, again. Chess is not a word game, but ChatGPT is trying to play chess using words, and it got confused. I did play the “b4” move, which looks like the Evans Gambit, but I actually played it one move later than normal, but that nuance was lost on the AI engine. The computer move “Bxb4” is a good move in the real Evans Gambit, but is terrible when played one move later. Similarly, the move I wanted to play would be illegal in the real Evans Gambit line, but is not in the modified version that I played.

There are several issues causing these problems:

1. ChatGPT hasn't been fully trained on all chess openings (e.g., my delayed “b4” move is an uncommon opening that it clearly hasn't been trained on), and
2. There's no “chess engine” being used, so ChatGPT is relying only on words.

Both of these issues are easily fixable, because there are whole books of chess openings available, and even a simple chess engine would suffice to make a playable opponent (or, at least, correctly identify legal versus illegal moves).

Hence, I presume that ChatGPT will be smashing me in our next encounter.

## Bad Names

There's a running joke in the industry about all its bad names. You'd think that with an industry that's just replete with uber-brainy personnel, there'd be some much better naming choices.

Oh, wait, umm, maybe I just found the problem.

OpenAI openly jokes about their bad ideas for names, like “GPT-4o” for a massive model release that deserved a much bigger reputation. Sam Altman has been quoted:

*“We deserve the roasting we're getting for the names. We will do better.”*

At least, Google has got their stuff together with their “Gemini” models, Anthropic has some personality with “Claude,” xAI has “Grok,” Alibaba has “Ernie,” IBM was “Watson,” and NVIDIA now has “Dynamo” and “NeMo” software.

Actually, most of those names are great, so, maybe it's just OpenAI that needs to hire a marketing manager or two.

Really, the researchers were the ones who started the whole thing. It's not just product names lacking marketing panache. What were all those Ph.D.'s thinking?

Here are some real acronyms: RELU, GELU, SiLU, SwigLU, PEFT, NAS. The silver medal winner here is certainly “RELU” standing for “Rectilinear Unit” or something like that. All that RELU does is take negative numbers and make them zero. That's all. It just makes sure all numbers are non-negative. Why does it even need an acronym?



And some other real names for technological issues in AI: knowledge distillation, hallucination, catastrophic forgetting, kernel fission, tensors, model collapse, optimal brain damage, slimmable networks, exploding gradient, regurgitative training, zombie weights, lottery ticket hypothesis, and mechanistic interpretability.

The gold medal surely goes to Retrieval Augmented Generation (RAG). The leader author of the original RAG research paper, Patrick Lewis, is on record stating:

*“We definitely would have put more thought into the name had we known our work would become so widespread...”*

But it’s not all about obscure names. There are some research algorithm names that have some extra memorability: Transformers, MoE, LLaMa, LoRA, Flash attention, Medusa, Eagle, RoPE, NoPE, Mambo, and Hyena.

## Over-Alignment

Alignment with human wishes is a tricky problem. There are hundreds and thousands of papers on how to “align” the output of an LLM with whatever weirdness a human might want. Usually, alignment is desirable, and the main problem is to fix instances of unalignment.

Alignment is mostly a good thing, but also possible is too much of a good thing. Be careful what you wish for! If you tell an AI that you want to rob a bank, what response should you get:

- Assuming you’re joking and laughing with you?
- Taking you seriously and talking you out of the plan.
- Blocking or refusing to answer completely.
- Helping you to choose the best bank to rob.

So, the issue here is one of ethics. The usual solution for most LLMs is to code up a “refusal module” and it will refuse to answer this query. Or, rather, it will have been trained to emit a politely worded refusal, rather than detailed instructions on how to go about your task.

Over-alignment is also possible and it’s known as “sycophancy” in the trade. In April, 2025, OpenAI had to roll back a version of their ChatGPT model because it was too sycophantic in its responses. They followed up with a couple of detailed research analyses about what went wrong.

# 3D Worldview

Visualizing what is happening in 3D is a subset of common sense. We understand what it's like to move around in a three-dimensional world, having done so since infancy. There are commonsense rules like:

- Two people don't stand in exactly the same space.
- Things fall down, not up.
- The walls of a room are usually vertical.
- A cup will sit on a table but not in mid-air.
- People can crawl under a table, but not through it.

I mean, 2D is hard enough for the poor LLM. There are all sorts of hidden rules for two-dimensional spatial data, like maps, GPS locations, printed pages, and computer screens:

- If you move North, then East, you are now North-East of where you started.
- The fastest way to travel from A to B is a straight line (in geometry).
- Typesetting usually should put text in horizontal rows.

Worse still, there are exceptions to apparently sane rules. If you go all around the Equator on a 2D map, moving right, you'll get to the other side of the map on the left.

Similarly, the fastest way for a jumbo jet to fly from New York to Paris is a "great circle" and not a straight line on the map. There's that 3D logic again, spoiling everything.

## Catastrophic Forgetting

You open up a chatbot session and you tell it your name, and the AI generates lots of useful stuff. Later, you open another session, and it doesn't remember your name. That's "catastrophic forgetting."

*Not really a catastrophe!*

But that's the official term and it's used in research papers, starting with Kirkpatrick et al. (2017).

It's not just between sessions, but also inside a long session. It used to be that the big models only had a "context window" with a 4,096 token length limit (i.e., a "4k context"). Once you get to the 4,097th token, it gets a bit fuzzy about the first one.

If you give the LLM a 100,000 word novel with 3,000 word chapters to analyze, it's forgotten what happened in the first chapter by the time it's moved onto the third one.

Fortunately, this isn't as much of a problem now with modern LLMs, and catastrophic forgetting has been long forgotten (LOL). Most modern LLMs now have a "long context" of 128K or more, and there's already a generation of "ultra-long context" LLMs that have a context window of one million tokens. Hence, LLMs are more like elephants than llamas now.

## Slowness

Most of the problems with AI engines and their weird limitations actually make some level of sense if you think about them this way:

*What tasks can the human brain only do slowly.*

Things like solving crossword puzzles and playing chess games are not automatic for our brain, but require us to logically think it through. They're using the "slow brain" rather than the "fast brain" mode.

There's the problem!


AI technology has solved the fast mode with wall-to-wall GPU chips, but is much weaker in the slow mode. The newer generation of "reasoning models," starting with GPT-4o in late 2024, are a step towards rational step-by-step thought, which are much better at math problems and crosswords, but they don't solve everything. Slow thinking is still a work in progress.

On the other hand, there are several limitations of AI models that humans can do fast. We have an innate understanding of 3D world layouts, and we know cause-and-effect at a very profound level.

Humans do these things fast!

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# 5. Neurology Versus Numbers

*“No, I’m not interested in developing a powerful brain.”*

— Alan Turing

## Neurology versus Numbers

The AI models are very similar to the human brain, since they are programming models of its neurons and synapses. There’s another similarity between LLMs and brains:

*Nobody knows how they work!*

Sure, there are neurologists who know about the brain, and technologists that know about AI models. But both areas are really quite underwhelming when you consider how little is known.

For example, neurologists really don’t know:

Why do we need sleep?

What causes dementia?

Incidentally, the answer may be the same: clearing away brain cell detritus. Our brain cells clean up waste by-products during sleep, and dementia may be an impairment in that process.

Anyway, technologists really don't understand their computerized AI models either. We can run them on huge computing clusters, and we know what they can do, but our understanding of *how* the models do these things is a little vague. For example, questions that AI researchers struggle with include:

Why do models lack common sense?

Why do they make stuff up?

Amusingly, the fact is that for every neurology area of study, there's a parallel research area in artificial brains.

## Activated Brain Regions

You don't use your whole brain all of the time. And I don't mean that "only 10%" rule that Hollywood is fond of. What I mean is that there are different regions of the brain that are "activated" by different activities. For example, we know about "lobes" in the brain:

- Frontal lobe (front) — high-level functioning (e.g., decisions, motor control, speech).
- Parietal lobe (top) — sensory inputs, numbers/mathematics, and hand-eye coordination.
- Temporal lobe (sides) — audio input, hearing, memory, and language understanding.
- Occipital lobe (back) — higher-level visual processing (e.g., detecting shapes and movement).

And there are many more sub-regions of the brain that have been analyzed in much more depth:

- Brainstem — basic life-preserving functions (breathing, heartbeat).
- Motor cortex — voluntary movement controls.
- Visual cortex — processing what they eyes see.
- Cerebrum — high-level rationality and logic.
- Cerebellum — movement and motor functions.



Neurology researchers have studied these brain regions in detail by: (a) the great joy of dissection, and (b) having people do different things while their brain is being watched by an MRI. You can literally see that different parts of the brain “light up” in response to different stimuli or when the brain is doing different types of work. Other parts of the brain are stuck in idle.

AI researchers are doing two main things in response to these types of neurology research:

1. Copying it!
2. Studying AI models.

I’m not sure which one came first, but AI engineers are doing both.

## AI Copies of Brain Regions

The brain’s structure is much more complicated than an AI model. In fact, whereas the brain has all sorts of different components scattered all around the skull, an LLM is rather simple in structure.

Your brain is rather special in structure, and un-symmetrical. In fact, the left hemisphere and right hemisphere do different things, which isn’t the case in AI models. Instead, the average AI model is rigid in its structure, and symmetrical in all three dimensions.

The “Mixture-of-Experts” or “MoE” architecture, as pioneered in GPT-4, is like dividing the AI model into brain regions. Different parts of an AI model get activated in response to different questions.

Firstly, note that experts aren’t chosen based on the whole question you ask them. It’s not like the model analyzes the input and then decides which part of the LLM will handle the whole thing. That’s not the Mixture-of-Experts architecture that I’m talking about here, although there is a different thing that does work that way, which is called “model routing.”

But here, I’m talking about having an LLM where internal submodels inside the model are turned on and off while it’s processing a response.

Note that the “experts” in an LLM are split on the strength of the signals along the “embedding dimension” of the matrices, also known as the “width” of the model. It’s not that one expert handles a word, and then a different expert does the next one, which is called the “lengthwise” dimension (or token dimension). Rather, each word is converted into “embeddings” as a type of “semantic vector” that gives it various weights on different signals (e.g., is it a noun like “cat” or is it a verb like “jump”). The model figures out which signals are strongest, and hence, which expert should process the data. Hence, simplifying greatly, a different expert would process a noun versus another expert that processes verbs.

You can see how this would be efficient. Having the DeepSeek R1 model would be slow if all 600 billion weights were used for every word. Instead, it only uses its 37 billion weights in each expert for each word. It’s potentially a different set of 37 billion, changing each time it goes around to output another word, but it’s still  $600/37=16$  times faster at each word, and hence, also that much faster for producing the whole output text. You can also see why this might be faster than GPT-4, which has about 200 billion weights in its experts, compared to only 37 billion in DeepSeek.

Vision and audio processing in AI models is very different in a sense (haha). There’s not really a full equivalent of the visual cortex in an LLM. Usually, the LLM doesn’t get a “raw feed” of vision or sound like the brain does, but instead gets one that’s already had factors like color and intensity computed for it.

Hence, the brain has some neuron power assigned to processing raw input signals, which the LLMs don’t need.

## Studying AI Model Numbers

AI researchers have been studying artificial brains in some depth, and you don’t even need to use an MRI to do this. In fact, you can just code it up. It sounds easy, but in reality, it’s a little tricky to analyze model weights, because it’s like trying to discern something interesting about what is literally a billion random numbers.

The whole area of studying AI weight numbers has a really great name: *mechanistic interpretability*. I’m not even sure what to write about that. I mean, sure, it’s interpreting the numbers, I guess, and they’re “mechanistic” in some way. Thankfully, most AI researchers shorten it to “mech interp” to hide the fact that they still don’t understand what the numbers actually do.

Nevertheless, AI researchers have discovered all sort of intriguing fact about LLM weights. These are just numbers, and they can be examined and also changed. Weirdness ensues in multiple ways:

- Attention sink — the first token.
- Layer importance — three levels of AI.
- Too many weights — thinning and shrinking numbers.

One weird thing is the “attention sink” research, which finds that there’s always one token that gets far too much attention: the very first one. So, the first word you use in a prompt matters a lot more than any other single word, and no-one really knows why that is. Maybe it’s not weird to think that AI only really listens to one word, because that’s how teenagers work.

Layers are another area of research. At the highest level is the study of “layer importance” in AI models. The structure of every model is that the computation goes repeatedly through several layers, sometimes hundreds, of identical number crunching.

Like in *Shrek*, layers.

The different layers of the model matter and they do different things. The early layers of an LLM do the high-level topic selection and guidance, whereas the middle layers start choosing the most likely next word to output. The final layers are “finesse” layers that choose between several good options for the best output.

Researchers have studied this by looking internally how the numbers change after each layer, and also by doing “layer skipping” or “early exiting” to see what happens if some of the layers are removed. Turns out that you can actually skip a lot of layers and still have a reasonable level of intelligence.

Maybe LLMs are only really using 10% of their AI brains?

## The 10% Rule

Could it be that LLMs are like humans and waste their brain capacity? It’s not actually a joke, because AI models are often shrunk to be smaller. Turns out if you have billions of numbers, and you don’t understand what they all do, then there’s some redundancy in there.

One technique is called “quantization” and that name is probably because it has *nothing* to do with quantum physics. Anyway, that’s the name of the most popular technique.

The goal is to make the model smaller, so it can run faster, while giving up some accuracy. In other words: a lot faster but slightly dumber.

Common levels of shrinkage, ahem, I mean, quantization, are from 32-bit to 4-bit, which is an eight-fold decline in LLM brain size. In other words, a 4-bit quantized model is only using 12.5% of its original brain power.

There’s also another way that is called “pruning” (good name) or “sparsification” (bad name), and involves setting numbers to zero. This is equivalent to “pruning” (removing) a synaptic connection between two neurons. In neurosurgery, this is done to block connections that are causing problems, such as in epilepsy, whereas in AI the weights are mainly removed just to get a speedup. Hence, different goals for pruning, but you can even combine pruning techniques with quantization.

So, yes, we can get below 10% usage of an LLM brain.

## Neurosurgery on AI Brains

Researchers haven’t just studied the numbers, but have also changed them. It’s like stimulating neurons in the LLM with an electric prod, just like they do in neurosurgery with Deep Brain Stimulation (DBS) to treat Parkinson’s disease.

The basic idea in AI research is called “activation patching” where you modify the outputs of each of those layers as things progress. If you change the numbers, then the output will change.

Note that this is not just about suppressing neurons, as in “sparsifying” the numbers by putting lots of them to zero. That’s a speedup, but activation patching is about changing the results, not just making it run faster.

What can you change?

Turns out, it’s not easy. There’s no simple algorithm to look at the numbers in an AI model and know what to change. Who knew that brain surgery could be so difficult?

Researchers have ways of changing the numbers, but they're not easy algorithms, and always involve watching the numbers first. The most fun you can have on a Sunday night in San Jose is running your AI engines and watching how the numbers change.

The most successful idea here is called “attention steering” or just “steering” for short. The idea is that you can “steer” the AI model to be more in some written tone, such as optimistic or pessimistic. The way this works is only in pairs of styles. The idea is that you run your AI engine with prompts that you know will cause optimistic or pessimistic outputs, and you know which is which. Then you look at the numbers from both, and run a “diff” on a big vector of numbers to find the numbers that are different in optimistic versus pessimistic answers. And that means the internal numbers along the way, not just the different types of words at the end, which would be too easy.

That difference vector is a list of numbers that is the set of activations that are different between the two styles. Hence, you end up with two vectors, one for positive, and one for negative. Later, when you want to do “steering” you can modify your model layers so that these extra numbers are added to the outputs.

Bizarrely, this actually works.

Unfortunately, it's hard to drill down deeper than this to give more steering control. We can find the signals that tend towards positivity or negativity, but we can't really identify the meaning of every number in the vector of numbers. Each number must mean something, or be a signal toward some output, but which one is what output?

Anyway, I mean, it's intriguing research, and I love it so much, but what's the practical point? It's easier to just command your AI to "please output in an optimistic tone" at the end of your prompt. That works, too.

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# 6. Fast & Slow Thinking

“Life moves pretty fast.  
If you don’t stop and look around  
once in a while, you could miss it.”

— *Ferris Bueller’s Day Off*, 1986.

## Fast and Slow Systems

The idea that there are two modes of thinking, fast and slow, was popularized by the breakout book *Thinking, Fast and Slow* by Daniel Kahneman, which spawned a whole discipline of behavioral economics, and won him the Nobel Prize. The general idea, greatly simplified is:

- Fast thinking — automatic and intuitive processing.
- Slow thinking — rational, logical analysis

These two systems also have other names:

- Fast — System 1
- Slow — System 2

And there's a distinction in terms of how we control the two systems:

- Fast — “subconscious” or automatic.
- Slow — “conscious” and intentional.

Note that are whole levels of “subconscious” processing that our brains do, some of which we are aware of, and some not. Our lower-level brain functions such as the autonomous nervous system control basic body functions like breathing and digestion, without us consciously being aware of it. With breathing, we can take it over consciously (e.g., swimming), but it always reverts back to automatic. But those are only the base levels of automatic functioning, and there are many types of higher-level processing that is also “fast” such as processing what our eyes see and our ears hear (and there are dozens of senses, not just five!).

Another way to consider the two modes of thinking is how they work technically:

- Fast — pattern matching.
- Slow — step-by-step.

Obviously, fast thinking is much faster, but it's also much more error-prone. Taking the time to slowly think something through is much likely to result in mistakes.

Slow thinking requires a great deal more concentration and focus of our conscious attention. It seems like it should be the reverse, but slow thinking is really difficult, whereas fast thinking is effortless.

## How Much Faster?

Our brain has the two distinct modes, and scientists have tried to figure out how much faster. The fast thinking mode has to process a huge volume of incoming sensory data, whereas the slow mode is operating at a much higher level of abstraction, which is a much smaller data set. Here's one set of statistics from Zheng et. al. (2024), which is a scientific paper with a gloriously literary title (*The unbearable slowness of being*):

- Fast mode — one billion bits-per-second
- Slow mode — 10 bits-per-second.

Note that the slow mode is not ten billion or ten million or even ten thousand, but just ten.

Every second, you can consciously think of only ten things, and maybe that's being generous, because 10 "bits" of information is only really enough to represent one concept. Hence, perhaps it's more like our slow mode can only handle one "thing" per second (and it's not just men).

Excruciatingly slow.

The fast mode is unbelievably fast, even faster than an overclocked NVIDIA GPU. A billion is a one followed by nine zeros. Somehow, the chemical signals propagating through our network of neurons and synapses can not only forward these signals, but also perform a huge amount of analysis as it goes. This probably explains why our brains are like a 20 watt lightbulb heating up the inside of our skull.

Certainly, the slow mode isn't using much energy. It's literally 100 million times less power-hungry than the fast mode. Solving physics equations doesn't use much in your brain, but sitting on the sofa watching TV is a lot more work, because it's invoking the fast brain mode.

## Fast Thinking

Fast thinking is where we look at a video and instantly know it's a cat. Or someone throws us a ball and we move our arm to catch it. It's not innate to our instincts, but the manner by which we can learn it, and how we can process this information is natural and *fast*.

Have you ever driven home, but don't remember doing it? Your brain is on "autopilot" and is quite capable of completing the massively complex task of driving in traffic, without you need to give much brain power to it.

Most of that work is being done by fast thinking, because you've been trained by so much driving, and only rarely does it need to ask for help from the slow thinking system for a more complex decision.

Your body is also controlled by fast thinking. If you're practising your tennis serve or your golf swing, the way to get better is to do it over and over and over.

They call it "muscle memory" but, come on, muscles don't have memory. It's your brain that has the memory!

In this case, the memory you're trying to create is a physical motion. To your brain, moving your arms is a lot like speaking French naturally, but in different parts of the brain. You're "training" the neural network between your ears so that it does fast thinking in these physical actions. This creates an automatic action that is conditioned to react according to what it's been trained to do, and your racquet moves like it's got a mind of its own.

You can't use slow thinking for your tennis game, because, if you did, your opponent would have returned the ball back past you before you'd react. Too slow.

## Slow Thinking

Slow thinking is the slower, plodding kind of thought. Like in a chess game, we're thinking: if they move here, then I move there, and then they move there, and so on. That kind of step-by-step logical thinking is slow thinking.

Incidentally, if you think that's the way to get good at chess, no, not really. Chess grandmasters are good at instantly recognizing patterns on the chess board, which is fast thinking, not slow. Grandmasters also know fast mode makes errors, so they double-check ideas for good moves from their fast brain, which is slow thinking.

We use our slow thinking mode many times per day in everyday life. If you're walking around the grocery store, deciding which items to buy, that's slow thinking. Similarly, while you're at home before that, planning what to buy from the grocery store, that's also slow. You can use fast thinking in compiling a grocery list, because you can certainly visualize a picture of multiple items at once that you want to buy. But when you decide to write them down, that's one at a time, and slow.

You can probably see a pattern here. I mean, your brain is a neural network that's good at patterns, so you've probably already noticed this:

- Images — fast
- Words — slow

When you "think in pictures," that's a fast way of imagining what to do. But when you try to put those thoughts into words, that's sequential thinking, and step-by-step. That reasoning is conscious and logical, one after another, and also slow.

Have you ever noticed you can't speak as fast as you think? Speech is actually a slow medium of communication. If we could "air drop" images from brain-to-brain, that would be faster. Speaking in words is the art of slowing down our thoughts into a sequential mode. Our brains are parallel, but our mouths are sequential.

# How Does AI Think?

Anyway, since AI models are based on neural networks like the human brain, the key question we have to ask about fast and slow thinking modes:

*Does AI have those?*

The short answer: yes and no. Fast, yes, but slow, no, not yet.

Fast thinking is neural networks and NVIDIA GPU chips and stuff. Slow thinking is still a work in progress. Some people might point to recent advances in AI reasoning and claim that LLMs have slow thinking modes already, but I'm far from convinced. I feel like that's still to come in AI research.

Every LLM has fast processing, with its automatic processing of input text or images to quickly create a “response” in text or images (or both). This overall version of reasoning, also called “decoding” of new tokens, is based on neural network processing, but coded in computer languages on GPU chips. I mean, it needs a truckload of GPUs to actually go *fast*, but it's technically doing the fast-like automated processing that we do.

What about slow thinking in AI?

Well, who knows. That's a whole different kettle of fish. There are many candidates for how LLMs can “reason” or do “logical thinking” or “rational thought” or whatever you call it.

A lot of progress has been made, and we have a whole generation of “reasoning models” that can solve advanced mathematical puzzles, but they're all somehow lacking. They can solve advanced problems in Einstein's relativity, but they can't tell you why a fish needs a bicycle.

Well, actually, I asked an AI, and it even got the joke.

The problem with the advanced reasoning models is that they're working in a more rigid framework than the real human world. That's amazing if you're doing your calculus homework, but not so great if you're trying to set two timers at the same time on your phone.

# Controller Mechanism

We don't really understand how our brain controls itself. There are all sorts of questions:

- How do we make decisions? (and why subconsciously biased ones!)
- What is sleep and which mode is that?
- How does the transition work from conscious to not conscious?
- How do we breathe both consciously and subconsciously?

Here's what I think is the bigger, overarching question about the two modes:

- Do fast and slow thinking modes cooperate?
- Or are they continually fighting for control?

Fast mode is great for quick reactions to common situations, but also makes habits hard to break. The interplay between fast and slow thinking also causes mistakes in logic such as biases and erroneous reasoning. Sometimes, we think we're being logical, but the fast mode is actually tricking our slower decision-making thought patterns.

Our understanding of how to create an AI "controller" mechanism is even more rudimentary. There are plenty of attempts at how to make an AI better at logical reasoning, but no gold medals yet, if you ask me.

## Fast Versus Slow Reasoning

Reasoning is an inherently slow and step-by-step process of thinking. Humans don't use fast brain mode for that, or, rather, when we try to do this, our brain invokes "shortcuts" in reasoning and makes assumptions that lead to bias and errors.

Same with AI.

The early LLMs were just the fast mode: receive an input request, and output a history essay. Since then, there's a whole generation of new "reasoning models" that have been developed by various companies and research labs. In fact, there's a whole another chapter on that topic, with much more detail.



There are two basic ideas:

- One-step reasoning — fast-like mode.
- Multi-step reasoning — step-by-step and slow.

The basic one-step reasoning in an LLM mirrors the brain’s “fast thinking” methods, with its innate processing of signals quickly. Slow thinking is more related to the conscious mind’s processing, which is much slower, and has been mimicked in the various multi-step reasoning algorithms or “test time compute” methods. Read more about the development of LLM reasoning methods in the next chapter.

## Hierarchical Reasoning Models

Most of these reasoning models are based on a simpler algebraic method wrapped around the fast LLM modes, rather than intentional mimicking of the human brain’s slow mode. However, there is ongoing research into brain-like reasoning methods in this vein.

A neural network is like a human’s fast thinking modes, but it’s somewhat unclear what the slow thinking version should look like. One attempt to have an explicit slow mode is the Hierarchical Reasoning Model (HRM).

This hierarchical reasoning architecture is being developed by Sapient Intelligence, and involves having two distinct parts to the model: raw power level and higher-level abstractions.

Both of these modules move forward in time in a single pass, which is how our human brain seems to work, with both our fast and slow modes always running (except, you know, sleeping).

Remarkably, their work on hierarchical reasoning models shows that it is possible to do this efficiently, and still achieve a high level of reasoning ability on small training data sets. Hence, this approach shows early promise.

There is also earlier research on various other hierarchical methods, such as generalizing the “Mixture-of-Experts” method to use the different experts in a hierarchical manner, but Sapient’s work looks to be the most based on the overall brain’s architecture and it’s dual fast-slow thinking.

# Subliminal Learning

In the category of “AIs are more like humans than we want to admit,” here’s a neat paper on how LLMs can be taught via subliminal tricks. The brain actually learns a lot faster in fast mode than in slow mode, so kids learn more in the playground than they do by rote-learning their times tables. Turns out, there are weird ways to manipulate fast learning.

Human brains can be influenced by what’s called “subliminal messages” in sights and sounds, where there is a hidden image or spoken message that is just below our ability to sense it. Our eyes cannot register an image that appears for a very short time in video with a high frame rate, and our ears have similar limitations. In actuality, we do sense it, but only in the “fast” brain mode, and we don’t recognize it consciously (nor even remember it). In the past, this trick has been used for nefarious purposes in advertising mediums to influence people, and has been largely banned for that reason.

Maybe we should also ban it for AIs.

This paper by Cloud et. al. (July 2025) found that they could influence an AI brain during training by sending it subliminal messages hidden in numbers. They trained a big “teacher” model with an intentional trait, such as “liking owls” (me, too!), by using standard prompting techniques (e.g., “You love owls.”). Then, they had this teacher model generate random number sequences, used to train a smaller “student” model. Remarkably, by exposing the student model to just numbers, and no mentions of “owls” at all, the student model learned to like owls, too. Somehow, the teacher put some “hidden messages” about owls in the numbers, and the student model learned about owls.

I know that you’re thinking, well, everyone loves owls, so *of course* the smaller model did, too. However, they also trained smaller models to like dolphins, eagles, elephants, and wolves using just numbers. Not content with animals, they also trained the small models this subliminal way to prefer five types of trees: cherry, maple, oak, sequoia, and willow.

Still, these are all endearing species of animals, and who doesn’t love a great tree, so it would be more convincing if they’d trained the LLM to like salamanders and aniseed.

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# 7. The Wall

*“It is by will alone I set my mind in motion.”*

— Mentat Mantra, Frank Herbert, *Dune*, 1965.

## Remember The Wall?

Do you remember when there’s was a lot of articles about how AI companies were “hitting the wall.” Several major companies were having trouble training their next-generation models, with only incremental improvements in performance found.

All the controversy started around November, 2024, with a flurry of media articles expressing concern about the big models. There was a two-fold indication that AI progress was “plateauing” or “hitting a wall.” The two main indicators were:

- Underwhelming progress in new frontier models
- Inference-based reasoning (“test time compute”)

The GPT “o1” model released in September 2024 wasn’t a bigger, more heavily-trained model with trillions more weights. Instead, it was a model that improved intelligence by doing multiple steps of inference, rather than one smarter step in an uber-trained model. This algorithm for “multi-step reasoning” was known as “chain-of-thought” and used repeated calls to process queries, before merging them together into the one final response.

Why did this change to multi-step inference for reasoning support the “wall” theory? Well, inference is a slow process when it runs, and “o1” was therefore slow for users — the line of logic was that OpenAI wouldn’t tolerate using this slow method if they could do it faster with one request to a bigger model. It almost seemed like a kind of “workaround” to hide training failures.

Hence, wall.

Secondly, there were also rumors about the big AI players are having difficulty training much better next-gen models. In particular, there were indicators that the GPT-5 release was having trouble gaining extra capabilities compared to GPT-4. Instead of OpenAI launching GPT-5 sooner rather than later, we were given “o1” with its multiple steps.

Obviously, training trillion-parameter models is a specialist field, and it’s evolving fast, with literally billions of dollars in funding being applied there. But open source models seemed to be keeping up with the leading commercial vendors (albeit, after a lag), which tends to indicate that there’s only incremental progress in reasoning capabilities, and the commercial vendors don’t have a huge “secret sauce” algorithmic advantage in training.

Some of the constraints include:

- Shortage of new high-quality training data (text).
- Complexity of software algorithms to train ever-bigger LLMs.
- Sheer volume of training data needed for multimodal LLMs (audio, images, and video).
- Capital cost of GPUs to crunch all that.
- Apparent lack of a new algorithmic advance in one-shot reasoning.
- Fundamental limitations of the way that LLMs and Transformers work.

There was also plenty of evidence to the contrary. OpenAI CEO Sam Altman posted on X that “there is no wall.” And there were certainly signs that many of the bigger players were still gearing up to use NVIDIA Blackwell GPUs for even bigger training runs. And there were two multi-billion dollar fund raises in just that month. So, the plateau was perhaps only a temporary thing.



Certainly, there was (and still is) a lot of research happening in training and in making LLMs better at reasoning in general. Some of the newer areas include:

- Newer GPU hardware for training (e.g., Blackwell).
- Faster software training algorithms (optimizing both computations and inter-GPU network traffic).
- Resiliency improvements to training (both software and hardware).
- Synthetic training data and derivative data.
- Multi-step reasoning algorithms are smarter (if slower).
- Long context processing seems to be a solved problem now.
- Inference optimization research (makes each step of multi-step reasoning faster).
- Next-gen architectures beyond LLMs (e.g., SSMs, Mamba, Hyena, and hybrid versions).

Nevertheless, the question at the time was whether there was a progress wall.

## Wall Obliterated

For a while there, it looked like there really was a wall. What a wonderful outcome for AI, because then all those billions of dollars in funding for training trillion-parameter models could now be redirected to making AI more useful and safe, instead of training for obscure benchmarks in advanced theoretical equations.

It's nice to have a dream.

Actually, no, the new new thing became inference at the end of 2024. This is exemplified by the recent OpenAI “o1” (“Strawberry”) model release in September, 2024, which was based on the “Chain-of-Thought” reasoning strategy. The basic idea was to run multiple LLM inference steps for every user question, rather than a “one-shot” attempt to answer the user. Over multiple repeating steps, the model could reassess its own output, and then converge on a much smarter answer.

It worked great. A little slow, but great.

But then the pendulum swung back the other way with the release of the DeepSeek R1 reasoning model in January, 2025. Instead of multiple steps of inference, it used “longer answers” as a way for the model to reason its way to an answer. It turned out that you could train an LLM to do reasoning better just by training it on a lot of such longer sequences, which it could then mimic. The result was smarter answers at a much lower token cost than multi-step reasoning. Who knew that “talking to yourself” would be an AI strategy for reasoning.

So, the wall debate was over largely before it got running, but it wasn't OpenAI that provided the sledgehammer. The release of the DeepSeek R1 model in January 2025 by a Chinese startup has largely ended the wall debate. Their model beat OpenAI's o1 model on multiple benchmarks (but not all), and did so using only single-step inference (whereas OpenAI o1 is multi-step inference). Hence, they used training advances to train a much smarter model than other single-step models.

Bye-bye, wall!!

Apparently, OpenAI knew this all the whole time, and I believe them. A research paper emerged from OpenAI within weeks of the DeepSeek release, where they presented research showing the advances possible in single-step reasoning.

Anyway, the point of all this is that there are now dozens of reasoning models, both commercial and open-source, that you can use to do anything. You can choose between one-step or two-step models.

On the other hand, there are still concerns about running out of training data, and also the long duration that it has taken for OpenAI to release the GPT-5 version. Unless all of these concerns are resolved, there's likely to be some more media articles resurrecting the theory of the wall, sometime in the near future.

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## 8. Data Crisis

*“We’re still in the horseless carriage era of AI applications.”*

— Tomasz Tunguz, June 2025.

### Training Data Sizes

AI engines are beasts that need regular feedings of new content to get smarter. They are continually searching for data, going out on safari all over the internet in search of prey. AI companies are looking for more sources of new data to train their smart silicon. Here’s some of the statistics on how much data they required:

- OpenAI GPT-4 — 6.5 trillion tokens
- Meta LLama-3 — 15 trillion tokens
- Meta LLama-4 — 40 trillion tokens

This data is expressed in “tokens” not words, but both metrics are somewhat comparable. For ChatGPT, a token is about three-quarters of a word on average.

Interestingly, a four-year old child only needs to hear about 40 million words to learn to speak. Probably, not as eloquently as GPT-4, but I mean, that’s a vast difference in scale: 216,000 times fewer words required than GPT-4 for a human brain (and over a million times more than used for Llama-4). The brain is a little better at learning.

# Data Shortage

How could the world be running out of data when there are so many kitten videos? Yes, although it seems to most people that the world is awash with endless content, the world is running out of *good* content to train AI engines.

There's a growing crisis. The world is running out of training content. Come on, people, we need to do better at recycling.

One aspect of the “wall” of training problems was a shortage of AI training data. The other aspect was concerns over reasoning models and software algorithms, as discussed in the prior chapter.

To humans, the size of the internet is vast beyond comprehension. But it's not actually that big for the LLMs, and they are training on a “crawl” of literally the entire public internet space.

Yum, yum. All those tasty Reddit threads.

But that was only part of the training data set for massive AI models. Vast databases of millions of scanned public domain books, not to mention a few pirated ones! The lawsuits about that are still ongoing.

There's not actually that much more content out there. I mean, we don't have ten extra internets to go crawl. New books are published at a rate of hundreds of thousands per year, but a hundred thousand books at about 100,000 words each is only 10 billion words, which won't even make an AI raise a sweat.

Where else could we find content?

# Synthetic Data

Synthetic data is computer-generated data that can be used for AI training. This doesn't necessarily mean AI-generated content, except that AI is probably the best technology we have for writing.

In fact, there are two ways that technology can create more AI content:

- New content creation
- Derivative content

Creating new content is obviously using LLMs or other writing technologies to create text (or images), that can be used for training. The other method is to take some existing content, and “derive” some extra content from that original content. This is also called “data augmentation” and various methods include:

- Machine translation — creating foreign language content.
- Synonymization — modify text using synonyms in place of the original wording.
- Summarization — create a shortened version of *War and Peace*.
- Paraphrasing — create versions that are similar but with different sentence structures.
- Sentence shuffling — reordering sentences in the text.
- Double translation — convert English to French and back again to get a variation.
- Noise injection — intentionally insert errors or mistakes to make it different.

There’s also a whole slew of similar techniques for video or audio data. You can augment images and video by changing colors or cropping, and audio data can have its pitch or other attributes changed.

Why is there a problem? There shouldn’t be a need to use any of these data augmentation techniques. I mean, if ChatGPT is great at writing content and creating images, surely we have an infinite source of content to use for training AI models? There’s only one major problem with synthetic data: it can make your model collapse in a heap.

## Model Collapse

What is model collapse? The term was coined by Shumailov et. al. (2024) in relation to models trained “recursively” on their own data. What they did was repeatedly output images and then re-used those images as inputs to train new LLM models. The result was that the accuracy declined every cycle, with the images getting fuzzier to the point where they were no longer recognizable.

Hence, the concern is where the accuracy of an LLM “collapses” if it is repeatedly trained on its own output. This is a major concern for large pre-trained LLMs that are trained on public datasets, because LLM created text is increasingly found on the internet, and may be scraped into these training sets.

The problem is the circularity, whereby LLMs are outputting new text onto the internet, which is then being re-used to train new capabilities in LLMs. If the theory of model collapse applies at scale, then this cycle will become problematic, with possible failure of the training logic.

Amusingly, the AI “slop” that is infesting the internet may also be annoying to the AIs. Seems somehow fitting.

## People Parrots

Humans to the rescue? How much data can one person produce? Let’s just assume we’re talking about textual information. What is the fastest way for a human to create data to train an AI engine? Let’s compare some ways:

- Typing — 60 words per minute (touch typing, not “hunt-and-peck”).
- Speaking — 240 words per minute (English), 360 words (Chinese).

I’m pretty sure I’ve seen young people on smartphones texting at about a thousand words per minute, but let’s not go there. So, talking. Let’s assume it’s a full-time job, which is around 2,000 hours (because we assume 50 weeks at 40 hours-per-week). Continual blather would therefore get you:

$240 \times 60 \times 2,000 = 28.8$  million words per person-year (English).

$360 \times 60 \times 2,000 = 43.2$  million words per person-year (Chinese).

However, we ideally want to create a trillion words, which is the order that these types of data sets are considered. How many people years?

- English — 34,722 person-years
- Chinese — 23,148 person-years

At an average salary of around \$60,000 USD annually, this amounts to about \$2.1-3.2 billion US dollars. That’s what it’ll cost to create a trillion original tokens of new human-sourced training content. Give or take. I wonder how much of that would be good content? The people will cost a lot more than the GPU cost of using new content to build our super-duper LLM, and the GPUs won’t need bathroom breaks.



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# 9. Reasoning Models

*“As the pace of AI progress accelerates,  
developing superintelligence is coming into sight.”*

— Mark Zuckerberg, June 2025.

## Reasoning Prompts

The first point about reasoning models is that you can get a long way with prompting. In fact, most of the early research on better LLM reasoning was just that you could get it to do better with a few tweaks to the prompts.

The classic example is the original Chain-of-Thought algorithm which was a single-step prompting method of simply telling the LLM:

*Let's think step-by-step.*

Surprisingly, this actually made the LLM think step-by-step, which was closer to reasoning than basic answers. There's a whole swathe of prompting strategies that you can use with your RAG application, if you want to.

The types of prompt engineering methods for improving the model’s ability to “reason” with more intelligence include:

- Chain-of-Thought (CoT)
- Emotional prompting
- Skeleton-of-Thought (SoT)

The relevance of all these reasoning-prompt things to your RAG application is that you can simply add words to your prepended system instructions prompt, if you want a more reasoning-ish RAG application.

## Chain-of-Thought

This is an advanced technique where the LLM can do better just with a little encouragement, like a toddler on a swing. The idea is to suggest via prompting that the LLM should generate a sequence of steps, which helps it to reason in steps.

**Step-by-Step.** In its simplest form, this is a method where the prompt has a helpful reminder prepended, encouraging that the LLM to proceed “step-by-step” in its answer. The idea is literally to include in the prompt an English sentence that literally says something like: *Let’s try step-by-step.*

More advanced versions of CoT use trickier prompting strategies. Complex prompting templates can be used to encourage stepwise refinement of multiple possible answers, so as to select the final choice in a more ordered way.

AI researchers are nothing if not copiers (e.g., they copied the human brain). Hence, everyone’s jumped on the bandwagon for technique names, and there’s also:

- Chain-of-Draft
- Chain-of-Tree
- Chain-of-Recall
- Chain-of-Verify
- Chain-of-Edit
- Chain-of-Symbols
- Chain-of-Tables
- Chain-of-Note

I have no idea what any of these are for, except that Chain-of-Draft is good at efficient reasoning, but feel free to look the rest up. Even better, come up with your own Chain-of-Bananas technique, and retire on patent royalties.

# Emotional Prompting

LLMs supposedly don't have emotions, and yet appealing to their emotional vulnerability seems to improve accuracy of answers. Anecdotally, some users had reported that they got better answers if they begged or yelled at ChatGPT. In November 2023, research was published confirming that LLMs did respond to “emotional stimuli” in the prompts.

The technique is to add an emotional sentence to the prompt. For example, to the text, append: *This is very important to my career.* Another one was: *You'd better be sure.*

Nobody thinks they've got emotions or become aware of their inner child. But somehow, the addition of emotive wording to a prompt triggered better working. Is there some kind of emotional signals in all that training data? Actually, the paper discusses why it works, and suggests a simpler explanation that the extra sentences add more definitive and positive word signals such as “important” and “sure.”

But they aren't very sure, although it's certainly important to their career. I cried when I read that paper.

## Skeleton-of-Thought Prompting

The skeleton-of-thought (SoT) method is from some recent research, and it has been getting significant attention in the literature. SoT is not just a reasoning improvement method, but has two goals:

- Smarter, and
- Speedier

The SoT idea mimics the way humans would write a long paragraph. Most writers don't just have the words stream out of their fingertips in one long writing session. Why should we expect the LLM to do that?

Instead, the SoT method is a multi-phase method that works in a human-like way:

1. Generate a rough outline (i.e., with paragraph main points or a list).
2. Process each sub-point in a separate LLM query.
3. Run a final LLM query to combine all the results nicely.

This few-shot method aims to generate a much better answer than a one-shot response. Each sub-point should get a more detailed consideration, and then the final output should be well-written. It's almost like a RAG architecture with a query for each sub-point, but the answers come out of the LLM itself.

Or, you know, why couldn't the sub-answers come out of a RAG system? Oh, wow! I just invented the multi-RAG multi-shot multi-model, which I'll now officially name the "manga" model.

Anyway, this combined multi-response idea in SoT isn't just more effective. It's also *faster*, because each sub-point can be processed in parallel. Each paragraph's LLM query can be running at the same time, although the first outlining query, and the final summarizing query, must still run sequentially. But still, that's three LLM query phases, rather than many more if there are ten sub-points in the answer.

Finally, note that although this is faster in terms of *latency*, it's inefficient in terms of *computation cost*. The parallelization reduces the time it takes to come back to the user, but all those parallelized sub-point LLM requests are chewing GPU juice. It's also not going to work well with "on-device" models, such as AI phones and PCs, where parallel capabilities are limited.

## Two-Step Reasoning

The advanced LLMs don't do all of their answers in one LLM inference sequence. In fact, they do many, and the state-of-the-art is "multi-step" reasoning. One of the basic multi-step methods is the use of "tools", such as:

- LLM devises a "plan" to execute the user's query, including tools to use.
- Execute the tools to get their outputs.
- LLM executes the final query to summarize the overall response, including any data from the tools.

This method has two LLM inference computations, whereas the "tools" are probably non-LLM code applications. This is assuming tools are doing things like:

(a) computations — e.g., a clock or calculator, and/or

(b) data source integrations — e.g., search real estate listing in a database.

Big LLMs have lots of calculation-type tools, and they also can integrate with a variety of disparate data sources. The issues of tool integrations and data sources are covered in a separate section.



# Multi-Step Reasoning

A more generalized idea for advanced reasoning capabilities is that the LLM makes a plan, which can include any number of other LLM sub-processing tasks. The idea is also called “few-shot” processing, because it allows multiple LLM calls, rather than “one-shot” methods, where there’s only a single LLM request. This is an area of state-of-the-art research in trying to reach AGI, by improving the LLM’s ability to plan and reason.

You usually don’t even know it’s happening if you use a third-party inference API to get answers to your queries. Which is good news if you don’t happen to have a PhD in machine learning.

There’s not always a clear distinction between one-step and multi-step reasoning. “Hybrid reasoning models” are LLMs that use a combination of single-step reasoning and inference-based multi-step reasoning. For example, Large Reasoning Models (LRMs) may be trained to use only a single step for some queries. Another example is that less powerful smaller reasoning models may be improved by using multi-step inference-based reasoning, known as “test time compute.”

There are many more prompting techniques, both zero-shot and few-shot, that you can research. Here is just a smattering:

- Rephrase and Respond (RaR)
- Re-reading (RE2) — appends “Read the question again:” and the question a second time.
- Self-Ask — encourages the LLM to ask “follow-up questions.”
- Memory-of-Thought
- Active Prompting
- Ensemble prompting — various multi-answer combination ideas.

Unfortunately, I’ve run out of electrons, so I’m not going to cover all of these. There are various huge survey papers on the internet if you happen to like strange nonsense that actually works.

# Deep Research Models

Deep research models are advanced LLMs that can complete complex research projects. They're kind of like multi-multi-multi-hop reasoning models.

Typically, deep research models will search for information on a topic, and then perform a reasoning function on the information. Advanced models may use multiple steps of information search and reasoning to refine their answer. There are several commercial models available that can perform deep research tasks, including:

- Google Gemini
- OpenAI Deep Research

There are several main architectural components that are key to a deep research model:

- Web search plugin (“web agent”) or other information source
- Large Reasoning Model
- Multi-step reasoning algorithm (e.g., Chain-of-Thought)

There is also an overarching algorithm that controls the whole plan. This may be LLM-based planning or could be other non-LLM heuristics (or some combination of both).

Deep research models are not cheap to run, because they have to process lots of information, and perform multiple reasoning steps. There is also the cost of information access, such as an internet search, although this would typically be less than LLM inference costs. There are various ways to improve LLM reasoning costs by reducing the number of tokens produced and processed by each reasoning step.

## Meta-Reasoning

Meta-reasoning is thinking about how to solve a problem. People say that AI is bad at “planning,” but I say that’s being quite unfair. The first order of business for an LLM that’s been presented with a user’s question is planning. Rather than thinking of the answer, it should first think about the *plan* for how to answer.

The decisions it needs to consider (and be trained about) include:

- Whether to invoke a “tool” such as a clock or calculator.
- Should an internet search be done?
- Is a query of a “plugin” required?
- Does it need a chunk of a company-specific document (in a RAG system)?

I’m a little vague on the difference between a “tool” and a “plugin.” And isn’t an internet search kind of the same? And looking up a text chunk in a RAG vector database? They’re all kind of “tools” that you “plug in” to your LLM. Maybe it’s just me.

Anyway, all those integrations above all require an extra “step” or “hop” to some other integrated system. Not all queries require these steps. There are also other issues in relation to producing the answer directly from the LLM:

- What output format is required (e.g., text or HTML).
- Should the LLM refuse to answer this question?
- Should it ask the user a followup question before answering?

Want to know something funny? These are all the same! They’re just training. If you want an LLM to refuse a query, you train it with bad queries and nice words that are refusals. If you want it to ask followup questions to clarify ambiguous questions, you train the LLM with ambiguous queries along with brief answers that contain the followup questions. If you want the LLM to invoke the clock when you ask for the time, you have to train it with queries about the time and answers that contain tricky “tool tokens” that run the clock. We’re giving the LLM too much credit for being humanlike.

It’s all just words to the LLM. Planning, not at all.

The final option in “planning” a response to a user’s query is: *none of the above*. There are a lot of questions that an LLM can just answer immediately, without hesitation, and without consulting some other system. When it does this without any extra step, we say it’s using its “parametric knowledge,” because it’s only using whatever has been trained into the many billions of “parameters” that are the weights in its model.

Don’t worry if you don’t understand how that all works, because I don’t, and nobody else does. There’s just a bunch of over a billion magic numbers that can help you fold your pillowcases in origami patterns.

# Not Following Instructions

LLMs are great at following instructions, and it's largely considered a “solved problem” in AI. If you ask the AI to “pretend to be Gollum” or “answer in Klingon” then you can be fairly sure it will do so.

There's also a whole lot of research on *not* following instructions, because there are lots of answers that AIs shouldn't give. This whole area of theory is called “refusal training” and the opposite research is where users try to bypass the refusals, which is called “jailbreaking” the AI.

But recently, there was a weird example of LLMs having a totally different failure to follow instructions. The research by Shojaei et. al. (2025) at Apple found that LLMs could not use the information in questions to solve complex puzzle problems. This is a different type of “instructions” from the above:

- Procedural steps
- Abstract puzzle problems

Why did the AI fail? Well, it's all words to the LLM, and clearly the words in the question that described how to solve the puzzle couldn't be understood properly by the LLM. It's like it couldn't map the words given in the prompt to the steps it was using in its reasoning.

Part of me wants to say that maybe we need a whole different architecture that understands “concepts” better and that will be able to map words to concepts that represent abstract steps, and back again to words at the end. Surely there's a chasm to overcome here that needs a rewrite:

- Words
- Abstract concepts

The idea of not mapping words to reasoning steps seems somewhat reasonable, until you realize that reasoning models use words to describe their steps. In fact, they “think out loud” in words, whether it's doing a one-step or a multi-step reasoning method.

So, I wonder if I'm about to be taught another “bitter lesson” in having models follow solution steps in the question. Maybe the problem was just not enough training data where the solution was given in the problem. Maybe the AI engines was just not paying enough attention to the original question. I mean, who hasn't forgotten to read the whole question in a math test?

And there's also the fact that the basic level of LLM instruction following is simply based on training. LLMs don't follow even the most basic human instructions by themselves, but need a huge training set of examples of human instructions and the correct LLM output.

Then the poor AIs get smacked with a stick called "reinforcement learning" and "penalties" during training if they get the answer wrong. That's how they learn to speak Klingon.

Hence, I have a horrible feeling that this apparently huge hole in AI abstract reasoning, where the solution in the question is unusable by the AI, might be fixable with a few thousand examples of math quiz questions where they also contain big hints about the answer.

## RAG Reasoning

The level of recent research attention to "multi-step reasoning" is off the charts. We've now seen papers on "chain-of-X" for almost every word in the English language. And this has now started to make its way into RAG research, although it's not a flood of papers by any means.

Every implementation of a RAG application can use any of those advanced reasoning algorithms, which would probably make it 1% smarter and 100% slower. Arguably, the type of advanced reasoning problems that OpenAI Strawberry or DeepSeek R1 is better at solving are not really in the bread basket for RAG, but it's worth a try!

Nevertheless, there's room for some more research on RAG and reasoning. For example, does RAG with Chain-of-Thought work better if you prepend the RAG chunks at every step of the way, or is it better just to have them at the first step? We're yet to see that in a research paper!

## Implicit Associative Priors

There's a weird thing about LLMs where they shouldn't be good at something, but they are. If your LLM starts writing a story about a guy named Morgan, then the LLM will use the name "Morgan" again later in the story.

Everyone says that AIs are bad at "generalization."

However, if I change the first part of the story to be about a woman named Mary, rather than Morgan, then the LLM will dutifully write the rest of the story using the name “Mary” instead. The story will be changed in a very general way to use a different name and gender of the main character.

Sounds like generalization to me.

I can’t really see how this works. Also, it’s going to work regardless of exactly which word contains the name. I can add a few extra adjectives, changing its position, and the name will still get re-used.

Note that I’m not talking about “context windows” where it used to be that the LLMs would forget that name if it was 4,000 words earlier in the story. Rather, I’m asking the question: how does it know to output the same name? The first time, sure, it just chooses a random name. What about the second time? What is it in its training that tells it to re-use whatever name tokens appeared earlier in the story, rather than generating a random name each time.

The answer is called “associative priors,” and the LLM starts to learn to re-use tokens earlier in its context, rather than any fixed name. This behavior arises over the course of extensive training whereby the model is paying “attention” to the tokens in the previous text.

In fact, to learn to pay attention to tokens at an earlier position, there is a technology called “positional encoding.” Weirdly, this technology doesn’t actually try to tell the LLM which position is best, but positional encoding simply makes the numbers at *every* position a little bit different, and then the LLM *learns* which positions are important during training.

Don’t worry; nobody else understands how this works, either.

Somehow, the combination of weights and “positional encoding” allows the LLM to re-use words from earlier in the text. Eventually, after passing a lot of training data under the bridge, this generalizes not just to know what words fit after other ones, but also to the higher-level answer of re-using the existing tokens at an earlier position, irrespective of the value of those tokens.

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# 10. Concepts

*“Learning to fly is not pretty  
but flying is.”*

— Satya Nadella, *Hit Refresh*, 2017.

## What are Concepts?

It’s a good question and there’s not a really satisfactory answer. If concepts were a simple concept (haha), then AI reasoning models would be a lot easier to build. The basic ideas about concepts include:

- High-level meaning
- Semantics not syntax

Concepts are about meaning, not words. There are also different levels of concepts, such as:

- Basic things — e.g., nouns like “cat”
- Basic actions — e.g., verbs like “jump”
- Abstract meanings — e.g., “symmetrical”
- Emotional meanings — e.g., “happiness”

As you can see from the above, it's not really clear what a concept really means (i.e., the “concept of a concept” is vague!). However, there's one thing that's clear about concepts:

*Humans are better at concepts than AI models.*

Maybe words are the problem. Humans think in images and relationships and concepts, whereas words are somewhat plotted onto these ideas.

Hence, there's a whole area of LLM research about having them think in “concepts” rather than words. The idea is to still use “tokens” but to have these tokens represent higher-levels as “concept tokens” rather than just words.

The terminology for AI reasoning about concepts is usually called “latent reasoning” because it's done in the “latent space” of abstract representations. I guess that's distinct from the “word space” where most LLMs are stuck at the moment.

The idea of concept tokens is not especially revolutionary. After all, in the theory of AI, we've already had:

- Stop tokens
- Pause tokens
- Formatting tokens
- Control tokens
- Separator tokens
- Fine-tuning tokens
- Tool tokens

Hence, yeah sure, why not have concept tokens.

In fact, concept-level tokens are used in several major areas of AI intelligence research:

- Prompt tuning (“prefix tuning”)
- Chain-of-Thought decoding tokens (“reasoning tokens”)
- Large Concept Models

Prompt tuning is a way to make the AI smarter by adding some special concept tokens to the input. This provides extra context to a user's question that allows the LLM to better understand what it's “reading” in the input context.

Reasoning tokens have been used as way to speed up the multi-hop reasoning models. Hence, they are more about efficiency than adding extra intelligence, though obviously the overall reasoning model is about adding capabilities. However, imagine what might be possible if you started with a rewrite of the architecture and put a lot of concept tokens together in a big model.

## Large Concept Models

The development of Large Concept Models, or LCMs, was pioneered by Meta in December, 2024, from its Facebook AI Research lab (Barrault et. al., 2024). As you may have correctly guessed, LCMs are models that:

1. Use concept tokens, and
2. Are large.

The LCM built by Meta operates on concepts at the sentence level. Hence, it tries to understand written sentences, rather than individual words, to discern the one or more major concepts that a sentence aims to describe. They train models using a huge amount of data, with over 2.7 trillion tokens of input training sets.

This approach generalizes the use of concept tokens from their specific uses as reasoning tokens in multi-hop inference, and prefix tuning with concept tokens as extra non-word prefix tokens in prompt engineering.

Concept tokens are central to LCMs. They are trained in concept tokens, and also perform inference in the concept token space. Hence, they're not using the old-style "word tokens" as used by most LLMs today. Nevertheless, LCMs and LLMs have the same types of uses:

- Generating text or answers
- Summarization of inputs
- Reasoning about answers

As shown in various research papers, this idea is workable at scales both small and large. Large Concept Models may indeed be a major step forward beyond the simple tokenized LLMs. The main advantages of using concepts are that the resulting models are:

- Smarter — better understanding of concepts and ideas.
- Faster — fewer tokens to process, because each token is "bigger."
- Understandable — you can trace what concepts were used to answer.

However, LCMs are still in the early stages of their theory, and even the Facebook paper says they are offering “an attempt at an architecture” rather than a finalized technology. One of the areas of difficulty in this method is to train an “encoder” that converts sentences into concept tokens. This encoder has to do “sentence-level embeddings” analysis. Maybe we’ll be going back to 2017 with an encoder-decoder architecture soon.

LCMs are certainly interesting, and they are one possible candidate for an extra leap needed to advance further towards achieving AGI. They’re competing against other “next-gen” ideas for AI intelligence, such as:

- Reasoning models
- Symbolic execution
- Knowledge graphs
- State Space Models (SSMs) such as Mamba and Hyena.
- Embodied AI models

Time will tell which ideas win out.

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# 11. Reading & Writing

*“If you don’t have time to read,  
you don’t have the time to write.”*

— Stephen King.

## AI Reading and Writing

Humans and AI engines share a strange commonality in how they communicate. As a human with the ability to both read and write, there are two somewhat related facts of life:

- It’s easier to read than to write.
- It’s easier to understand a foreign language than to speak it.

Weirdly, this turns out to also be true for AI engines. The coders for AI engines have done a lot of work in both areas, but reading remains easier than writing.

In the olden days, which is 2017 in AI, the LLM engines based on the “Transformer” architecture (discovered by Google) had two explicit pieces, called the “encoder” and “decoder” components.

The idea was basically:

- Encoders — reading
- Decoders — writing

The encoder would take its input text and “encode” it into some internal vectors, which are used to “understand” the text (i.e., reading). The decoder would then use these internal numbers to emit new numbers that represented words that it was outputting (i.e., writing).

However, that combined encoder-decoder architecture didn’t last long, and the encoder was found to be mostly redundant, since it was doing the computations that were very similar to the decoder, only it wasn’t actually decoding anything. Confused? You’re like most AI engineers, if so. Anyway, you could do both the reading and writing inside the decoder, by doing a trick called a “prefill” phase.

No need for half the brain.

Hence, the encoder was removed from AI engines and only the decoder was left. This was called a “decoder-only” architecture and was used as early as the GPT-2 model. The newer idea is effectively:

- Prefill — reading
- Decoding — writing

Prefill is an algorithm that runs in the decoder, so these two phases are running in the same GPU chips (well, no, but let’s assume that for now). The decoder in the newer decoder-only architecture is similar to that used in the encoder-decoder early version, but obviously doesn’t need the parts that used to accept data from the encoder (which no longer exists).

Have we lost something by not having an encoder? It’s certainly possible that some insight is missed by treating reading like it’s a subset of writing, rather than trying to fully understand first. However, we gained: speed.

We need a lot more speed to do advanced data processing, such as voice or video analysis. It’s all just data to an AI engine, but there’s much more data in audio and video.

The way it works for speech models:

- Understanding speech — “reading” of voice numbers.
- Speaking — “writing” of audio data (i.e., decoding).

Again, there’s not usually an encoder for voice models. But don’t worry, because the poor old encoder component didn’t get completely thrown into landfill. Encoder-decoder architectures are still used for some two-phase type operations like foreign language translation, where we’re reading in one language and writing in another. In these cases, the reading is very different from the writing, so having two separate components works well.

## Prefill for Reading

The way that prefill works doesn’t really make sense compared to human reading. The AI engine looks at every word in its input prompt and processes them all at once, in parallel. The reason it can do this is that this phase does not output anything, and is really a preparatory phase before writing.

What’s it prefilling?

The reason it’s called “prefill” is that it fills in the “KV caches” for the input tokens (e.g., the user’s question). These are extra numbers used by the second phase, the decoding phase, to figure out which new words to output.

Humans can actually do this type of parallel reading that AI does in prefill, but it’s not the natural way that we read. If you train yourself, you can actually start reading a novel by scanning multiple lines at once, across the page, like you are ingesting groups of words as they cross your visual field. It’s hard to learn, but it can be done (by humans).

GPU chips are naturally parallel, and AI engines can read all the words of a document in parallel without even blinking. The LLM ingests all of the words at once, and then cross-analyzes them to find relationships between the positions with all the other words.

This is all done in parallel in the prefill phase, analyzing all of the inputs, before it starts emitting words in the decoding phase.

# Decoding for Writing

If you read about LLM theory, you will discover that the way that an LLM writes text in the “decoding” phase is to output one word at a time. It only looks backwards to any of the previous words, and figures how the probabilities for each of the possible next words, and then chooses the best one. The decoder is actually “masked” so that it doesn’t look ahead, and anyway there’s nothing up ahead anyway, and it only looks backwards, and never backtracks.

This is total baloney.

It may have been true in the very earliest theories of neural networks, but modern LLMs do a whole smash of other stuff in their decoding algorithm. I mean, you can’t write a good piece of prose based only on past words, especially if you only ever look one word ahead.

Humans do writing by thinking forward many words, revising, going back and changing, and so on. Hence, in reality, your LLM does a lot of coding tricks to decide on the best words to write:

- Trying multiple possible word sequences (in parallel).
- Backtracking and restarting phrases and sections.

There are some fancy names for some of these algorithms, which mostly run in parallel on GPU chips:

- Beam search
- Speculative decoding
- Multi-Token Prediction (MTP)

Beam search is about running ahead a few words, checking whether it’s any good, and then backtracking. Speculative decoding is about trying multiple possible new phrases to write, all calculated in parallel.

Multi-token prediction is about emitting more than one word at a time, usually also combined with beam search or spec dec (that’s short for speculative decoding).

Humans struggle to do this, although there are probably some people who can speak more than one word at a time in parallel. Strangely, an image of Elon Musk just popped into my subconscious brain. But I digress.

All of these decoding methods are done in parallel in the “forward pass” of the decoding algorithm. This is like the “fast thinking” mode of writing, and are not really doing advanced rational logic or any higher-level analysis of the words.

In some of the fancier models, there’s also a second “slow” method of revising the output, whereby the LLM can itself make changes to what it’s written, or possibly have an even bigger model check over its work. That’s like your English teacher peeking over your shoulder while you compose your persuasive writing essay.

## Reading Limitations

Reading doesn’t mean understanding. The LLM is reading the words as “tokens” that represent the text. There’s also tokens for images, audio, and video, which are more complicated, but still the same basic architecture. A voice LLM sees your speech patterns as just numbers, too.

Words are actually a higher level abstraction than the numbers in voice or images, so they should be easier to interpret. However, the problem with reading words is that all the LLM knows about is words. The meaning of words is often obscured, and there are problems with simple things like representing numbers as words, which makes it hard to do basic arithmetic.

Understanding of words also implies a lot more things than just text patterns. There’s hidden meanings in all sorts of ways using rules that humans know, or have learned. For example, how do you know that it’s a joke that we “drive on parkways and park on driveways”? LLMs are bad at jokes or sarcasm without special training.

Common sense is also hard to explain in words. It’s like there’s a mapping between pairs or groups of words. For example, cats are “svelte” but not dogs, or we “sit on sofas not tables”, but there are all sorts of exceptions to all those so-called rules.

Our world is difficult to describe in words, because it’s three-dimensional. Babies learn that if they try to crawl under a desk, they might smack their head, because one failure gives them a powerful learning signal involving lots of noise and cuddles. How does an AI know what three dimensions are? It’s not in the word patterns.

The fourth dimension, time, is also tricky. Food appears on a plate and then disappears, not the other way around, and yet both ways it would have the same words. They call this “temporal reasoning” and, since it has a fancy name, that means it’s a research area with lots of difficulty and plenty of obscure research papers. AI models are not good with time. In contrast, a human child moves through time intrinsically, and comes to understand that idea at a very deep level.

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# 12. 'Rithmetic

*“Math skills are a powerful indicator of future success.”*

— Bill Gates.

## Everyone Loves Math

Humans are great at arithmetic! Right from birth, we can add up 10-digit numbers in our heads, without even using our fingers and toes.

Umm, no.

Weirdly, AI is bad at arithmetic, too! Maybe it's not so weird, as we've been discussing the parallels between brains and LLMs, but it definitely seems funny.

Surely, computers can do basic sums very easily?

Yes, indeed. Your average laptop computer is running a CPU that has a clock speed of about 1 or 2 Gigahertz, so, let's say it's about 2 billion operations per second. And the most basic computer instructions are addition and multiplication operations. In fact, those are the simplest of arithmetic operations, but there are all sorts of other maths stuff, too.

If you have an older laptop, it can only do “32-bit” operations, which is numbers up to about 2.7 billion, which are at most 10-digit numbers. But most modern laptops are now using “64-bit” CPUs, which allows up to 19-digit numbers. To help you win *Trivial Pursuit* next Saturday at your AI club meet, note that a trillion has a one followed by 12 zeros for a total of 13 digits, a quadrillion has 16 digits, and a quintillion has 19 digits.

So, your basic laptop from Best Buy that you can buy on a credit card for less than the cost of a pet parrot, can do perfect arithmetic in massive numbers up to quintillions using at least 19 digits, and do so with 100% accuracy, over and over, billions of times per second.

An LLM can’t.

Every LLM is great at detecting patterns and knows about words. In fact, it usually treats a number as a word, and a 10-digit number will likely be 10 words, one digit each. So, the LLM will have seen “sentences” like “ $1 + 1 = 2$ ” in its training, so it’ll nail those ones. Unfortunately, it’s expensive to train it to recognize all the different “words” up to a billion, let alone a quintillion.

Infinity is a little problematic.

If you’re thinking that it’s smart enough to figure it out from the other sums it’s been trained on, well, I beg to differ. LLMs have been historically poor at “generalization” of patterns. For example, if it knows the pattern “ $1+1=2$ ” that doesn’t mean that it knows the pattern:

“ $1,000,000,000+1,000,000,000=2,000,000,000$ ”

Not at all, unless it’s seen that exact pattern in some other training document. A human child does this extrapolation of patterns innately, but your average multi-billion-dollar LLM struggles at this very hard stuff.

Okay, before every CEO of an AI company sends me a nasty cease-and-desist letter pointing out that their trillion-parameter LLM can do sums just fine: yes, they’ve figured it out now. But for years, LLMs were bad at basic arithmetic, let alone more advanced math, and there were research papers published all about the problems with basic arithmetic and complex math. So many.

And, honestly, LLMs are still poor at arithmetic, but there’s a couple of workarounds. One is “reasoning models” that can do multiple steps to solve a problem, which we discussed in a separate chapter.

However, although I don't know for sure how it does it in the big LLMs, I'm betting it's the second one:

Tools.

If you submit a couple of 10-digit random numbers to your favorite AI assistant and ask it to multiply them, it's probably not really the neural networks doing the number-crunching work. More likely, it's a special "tool" known more formally as a "calculator," which is linked up to the LLM itself.

So, behind the scenes, the LLM notices that your request looks like it needs a calculator, because it's good at recognizing patterns like that, and then calls the internal calculator tool without telling you.

The calculator tool is not using neural networks, so it's literally a billion times faster than the LLM, and you won't notice any delay from the extra step. Incidentally, I'm referring to the grunt-work calculator tool inside the AI servers next to the LLM code, not the graphical one that you can launch on your laptop or smartphone.

After this extra hop, the LLM then combines the output from its calculator tool into a lovely couple of paragraphs, the last of which wraps up with an optimistic offer to "explore" its answer further, should you so wish.

## Symbolic Execution

For some strange reason, the programmers that wrote AI engines thought it might be a good idea for an AI to be a programmer in order for it to get smarter. I mean, if I want to train my LLM not to put "rocks" on the grocery list, obviously it would do that better if it spoke to me in Python.

Anyway, here we are: symbolic execution.

Having the model interface with a "symbolic interpreter" or other symbolic representation is one way to improve a model's reasoning capability. There are various different approaches, ranging from very mathematical logical languages to more compute-related dialects such as executing Python scripts.

In this idea, the LLM generates Python as its output, which is then interpreted by a built-in integration. If you prompt the AI with this:

```
This a test.
```

Then the AI will generate this intermediate Python program to run:

```
print("This is indeed a test.")
```

This is a silly example, because LLMs are certainly smart enough to do different things for different input prompts. Simple prompts do not need symbolic execution. The idea with symbolic execution is that simple prompts are handled the normal way, without coding, whereas complex reasoning type inputs are handled indirectly by generating an executable Python program.

There are some reasons why this indirect approach of generating answers via symbolic execution might work well, at least for a subset of problems. For example, Python programs are more general than LLM's decoding algorithms:

- Looping-type constructs in programs.
- Hierarchical or recursive logic.
- Second level of indirection capability.
- Turing completeness of computation.

Turing completeness is an obscure Computer Science theory about programming languages, where they must have:

1. Sequence — execute two statements in a row.
2. Selection — an “if” statement that chooses two paths.
3. Iteration — looping around to do it again.

There's actually a fourth requirement in practice that's sometimes overlooked in the theoretical treatises:

4. Persistence — ability to store data somewhere (i.e., variables in memory or disk).

LLMs by their lonesome are actually *not* Turing complete, because they are finite, which means that they miss the third capability. LLM models are a fixed-size data structure with very little looping or “iteration” capability.

LLMs are massive, yes, but still finite.

On the other hand, LLMs have all the other requirements, and using a multi-step reasoning algorithm around an LLM can add that type of non-deterministic looping. So, maybe that’s all it needs to be Turing complete.

Symbolic execution has not yet really taken off as a way to improve LLM intelligence, although there are some startups still working on this idea, so who knows where it might go?

Perhaps coincidentally, instead of learning coding making the LLMs smarter at lots of stuff, LLMs got really good at coding, to the point where the job that is now considered most likely to be fully replaced by AI engines: *programmers*.

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# 13. Tools

*“Right now, I think the frontier is these AI tools.”*

— Sam Altman, July, 2025.

## What are Tools?

Humans like to think that we are distinct from the “animals” because we use tools. Sadly, this does not distinguish us from the AIs, because they’ve also evolved to use tools.

LLMs require tools to do more advanced things, just like humans. For example, if someone asks you the time, you look at your watch (or your phone). If you ask an LLM "What is the time?" there is nothing in its training data set that could possibly answer this correctly. The only way is to use a tool called a “clock” and it must be integrated into the LLM, and executed by the AI Engine as part of answering your query. Some of the things that are hard for an LLM to do without tools include:

- Having real-time or up-to-date information (e.g., stock prices or the latest AI research papers).
- Computation-related questions beyond basic arithmetic.
- Information that’s only in a different place (e.g., the company’s internal ERP database).
- Time-specific or locale-specific information that differs from its training.

Another type of tool that LLMs can use are those that perform an action for you, such as sending an email. These are called “agents” in the AI industry, rather than “tools” as the terminology.

That’s not where the naming confusion ends. The AI research industry seems to make some distinctions about several different types of tools. For example, there are these AI research areas called:

- Retrieval Augmented Generation (RAG) — find a paragraph of text from a set of documents.
- Tool Augmented Language Models (TALM) — run a dynamic computation tool like a calculator.
- Tools “Hooks” — run a dynamic preprocessing tool on your text input.
- Plugins — log into someone’s database for information (e.g., real estate listings).
- Search plugins — run a full internet query to return some blue links for AI to read.

Come on, they don’t need different names when they’re all just tools! The AI engine calls out for help from one or other of these various different pieces of software, whether it needs a BMI calculator, a corporate HR document, or a full search of the internet.

Well, maybe there is a key distinction between two different classes of “tools” if we exclude the “action agents” types, and focus on tools for helping the LLM just to answer questions:

1. Look up more information — RAG, internet search, database plugins.
2. Dynamic computations — clocks, calculators, and many more.

One way to think about this: static search tools are looking for extra human-written information, whereas dynamic tools are creating their own! Types of dynamic calculation tools include:

- Clocks
- Calculators (arithmetic)
- Converters (e.g., pounds to kilograms)
- Calendars (date or day calculations)

Modern LLMs use literally thousands of tools. All of these tools are pieces of software that sit alongside the AI model in the backend servers.

AI engines don't normally tell you what tools they've used to answer. How unfair is that! We're not allowed to use AI to answer questions in job interviews, but the AIs are allowed to sneak around using any tools they like.

There are a lot of tools that an AI can use, far beyond the basic ones. For example, if you ask your AI engine to compute the “Flesch-Kincaid” reading level metric for a paragraph of text, it has to use a tool to compute that.

## Integration of Tools

There's a lot of variability in architectures for using tools, but the basic ideas are to use them for:

- The beginning — preprocessing (“hooks”).
- The middle — interim computations.
- The end — finalization or formatting.

The main one is the muddle in the middle. Your LLM will run a sequence something like this:

1. Read input prompt ("Should I eat jelly beans in order of wavelength?").
2. Decide to get the results of the tool.
3. Insert “tool tokens” into the output text.
4. Run the tool or tools (by finding tool tokens in the LLM's output).
5. Merge the tool output into the final output text results.

Like humans, an AI needs to learn to look at its watch if someone asks the time. Specific training data sets are required that tell the AI what tool to use, and when. This is the “deciding” phase for tool usage.

The AI engine has to recognize in the LLM output that a tool must be executed.

There are a variety of ways to do this:

- Tool-specific tokens — i.e., the LLM can emit a “trigger” token to run a tool. Note that PEFT could be used here to fine-tune new tool capabilities, by only adding a few new tool-triggering tokens to the vocabulary.)
- Placeholder patterns — i.e., output something like an “--insert current time here--” special pattern is another way, and the engine then looks for these patterns, which avoids adding tool tokens to the vocabulary, but is inefficient in that there are multiple text tokens in the output).
- Code generation — there are various AI models that will generate code, such as in Python, that can be executed to generate the answer. This is a general solution, because Python can call various submodules and can thereby generate many tools.
- Multi-level planning — the AI first generates a plan of how to answer the query, including what tools to use, and then runs any tools, and then does another inference query to collate it into a final answer.

Sometimes, there are two steps of LLM inference being done, with both the deciding and merging steps above. Alternatively, the tool integration can be simpler with the tool’s output results just inserted verbatim into the middle of the output.

## Computers as Tools

Lately, there’s been a huge amount of work on LLM things called “GUI agents” or “computer usage models” in the AI space. The idea is that the LLM can actually look at your screen and tap away on your keyword and click the mouse, too.

Phones, too!

A computer or smartphone is a great tool for an LLM. Anything that a computer can do, the LLM can now do. Amusingly, it’s a really tough problem to solve, which is odd, since the AI engine is already running inside a great big computer. Lots of research papers! The technical issues to solve include:

- Understanding the screen (as an image)
- Integration with input devices (keyboard/mouse)
- Context of the screen at a high level (e.g., which app is running?)

There’s another major problem to solve: mistakes. LLMs always make mistakes, and that’s more of a problem if the agent is doing something for you on your computer.

# LLM Hooks

LLM hooks are integrations of tools that perform preprocessing on prompt inputs. The use of hooks is a special case of Tool-Augmented Language Models (TALM). The idea with pre-processing hooks is that the tools can augment the input prompts with extra information that the LLM can use, which is similar to RAG-based retrieval, but is based on non-LLM tools that perform dynamic computation.

Tool Augmented Language Models (TALM) is the use of non-LLM tools to augment the processing of LLMs. Tools can be used to compute more data based on the prompts, and can be used on conjunction with reasoning like Chain-of-Thought, RAG retrievals, or agentic architectures. Hence, the idea of “hooks” is a special type of limited tool, that doesn’t scour the internet for more information, but only performs some dynamic computation on the prompt text as input.

Using “hooks” to launch a tool to preprocess the user’s input prompt is a lesser-known technique. You can use heuristics to decide that a tool is used, and it’s called before the LLM via “hooks” in the code. This idea skips the “deciding” step above in favor of non-LLM methods. This is faster than having an LLM decide to launch a tool, but it’s not always as accurate in choosing whether or not to use a tool.

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# 14. Brainy Body

*“A strong body makes the mind strong.”*

— Thomas Jefferson.

## Brain Versus Brawn

Do you need a body to be smart? It sounds somewhat facetious when you write it like that. And yet, it’s a serious question with a whole slew of research papers behind it, titled: *embodied AI*.

Technically, I’m mainly going to talk about the theories of “embodied cognition” and the achievement of real intelligence. There are other practical aspects in physical AI such as sensory capabilities (e.g., machine vision) and having robots that have mobility and the ability to take actions (i.e., go somewhere and do something).

This research about embodied cognition espouses the theory that achieving true intelligence requires physical interaction with the world. In short:

*No brain without a body.*

Why might full intelligence require a physical presence in the world?

Some of the reasons a physical body is required include:

- Self-awareness (of oneself and one's dimensions)
- Building a theory of the 3D world
- Generalization of world-based reasoning

Another obvious reason is for an LLM to actually understand the human senses. Any good writer of fiction knows to use the five senses for “show not tell” in a scene:

- Sight (vision)
- Sound (hearing)
- Smell (aural)
- Touch (tactile)
- Taste (gustatory)

You know there are more than five senses, right? I'm not being supernatural, but refer to all the weird extra senses that our bodies actually have, including:

- Physical sensations — pain, discomfort, butterflies, tingling, numbness.
- Body states — hunger, thirst, nausea, fever, illness, dizziness, etc.
- Proprioception — knowing the position of our body in 3D space (my favorite one!).

There's a bunch more. Apparently, humans can detect magnetic fields, but not as well as pigeons. Except for that weird one, you know all of these extra senses, innately, without having to be trained or sent to boarding school.

How many does your LLM understand? None.

It is more than a theory that LLMs should reside in physical robots, such as to achieve mobility or allow actions to occur, but that their *training* must occur in this way so that the LLM can itself be intelligent in a more complete way.

Maybe boarding school for LLMs is worth a try.

# Why Embodied?

Think about how a baby learns. They reach out into three-dimensional space learning where everything is, including their own personal space. Later, they crawl around, learning how things are arranged in the world, and what it feels like to touch anything they can find, to their benefit or their peril.

How can an LLM do that? All it has is its words. Can we really explain all of those things to an LLM by giving it more words to read? How is it to learn the meaning of this joke (and is it a joke?):

Kemp's Law: *Never re-tie only one shoelace.*

An LLM is inherently stuck inside its own head. Indeed, embodied AI is one of the theories about why modern LLMs still struggle with various aspects related to human-level intelligence:

- Two-dimensional spaces (e.g., chess boards or *Galaga*).
- Three-dimensional reasoning (e.g., people sitting at the kitchen table).
- Textures and senses (e.g., how it feels to touch or smell).

Is automated driving of a car in a 2D or 3D world? The answer is: yes, both. There are aspects of 2D maps, certainly, for efficient execution and specification of certain tasks such as pick-up, drop-off and routing. However, for safety the LLM must consider its full three-dimensional shape and the same of the other vehicles and their overall environment.

The benefit of real-world experience is not limited to physical ideas about a multi-dimensional environment and the objects it contains. Some of the more non-obvious limitations to full intelligence that embodied AI seeks to improve include:

- Self-awareness — the AI is in the environment, too).
- Temporal reasoning — time always flows one way.

Understanding of time and the notion of “causality” (cause-and-effect) may be improved by embodied AI. Learning about the world while experiencing real-time changes in the environment could improve an LLM's ability to reason about time.

# Fake Versus Real Bodies

Researchers have tried the old *fake it till you make it* style of research for embodied AI, although they don't describe it that way in their research funding proposals. Instead of a real body, we can pretend that scanning through a stream of video and audio data is the same as having eyes and ears. You can try to learn from that, and this is definitely getting better.

Training advanced LLMs on video data is a thing.

But what about real bodies? What about the senses of touch? Can they explore the world and learn what it means to be inside a 3D space? Do they feel pain when they fall off their bicycle?

Lots of robots have real bodies, and they're starting to look impressive, but do they learn?

As far as I know, no-one's really invented a robot hooked up to a smart enough LLM that it could learn. I mean, I could have written "learn as it grew" and there's a few Hollywood movies that I quite like where this happens, but not in real life.

Robot soccer is not quite there yet.

It might be a while before humanity designs an advanced mobile learning station.

Oh, wait! Sorry, I was wrong. We have managed to create something advanced that can learn like that:

*Babies.*



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# 15. Faster AI

*“You’re gonna need a bigger boat.”*

— *Jaws*, 1975.

## Faster AI

AI engines are already amazingly fast, but it’s not enough. LLMs are just not big enough, despite already being ginormous. How much computation is going to be needed for the next generation of even smarter models?

Lots more.

It’s not clear yet how far ahead we need to go into the future to get the capacity that’s needed. Processing AI computations on GPUs is continually getting faster. NVIDIA is now on an annual cadence of GPU updates, where each general release of silicon beasts gets faster and faster.

There are really two things that are getting faster:

- Faster training — baking braininess into brawny silicon chips.
- Faster inference — answering your queries and generating poetry.

The weird thing about the speed of AI engines is that there's really only one bottleneck.

It's a complex architecture, but most of the compute grunt is consumed in one small part of the code. AI kernel engineers are forever fiddling with about 1,000 lines of code.

## Endless Matrix Multiplications

You studies this in High School math class: matrix multiplications. Remember how you had a weird 2x2 square of numbers, and you had to multiple across a row and down the other column. AI is based on that type of matrix multiplication, and almost nothing else.

Who knew that High School math could be useful?

AI engineers like to make it sound more complicated than that. Our favorite word to use is “tensors” and we hope nobody realizes that it's just matrices, only more than one. Our 2x2x2 tensor in 3D just means that we have two of the 2x2 matrices.

Hence, when you see the press releases about how great NVIDIA GPUs are with “Tensor Cores” you can roll your eyes, and think: I learned that stuff in High School.

## 500 Ways to Optimize

There are over 500 ways to optimize an AI model. Not an exaggeration — I literally made a list and counted them. I'm not going to force you to read it here, but it's in the references. If you're a new parent with trouble getting the little one to sleep, feel free to read it to them.

The main bottleneck in AI is the above matrix multiplications, and everything else is secondary. Although training and inference are very different algorithms in AI, they both come down to matrices, ahem, sorry, I meant to say tensors. There's a lot of ways to improve things, but the main categories are:

- Fewer matrix multiplications
- Smaller matrices
- Different types of arithmetic

To do fewer matrix multiplications, we’ve already talked about a big one: Mixture-of-Experts. For example, the 600B model in DeepSeek is cut down into 37B experts, which is a lot fewer matrices every time it crunches out a new word.

Another way is to use smaller matrices inside smaller models. There’s an optimization called “distillation” and I wonder how it got that name? The idea is that you train a huge model, called the “teacher” model. And then you get the teacher to talk to another smaller model, so as to train it, or to “distill” the big model’s answers into the smaller one. It’s called the “student” and I’m not making this stuff up.

Anyway, the smaller model is faster.

Another way to get a smaller model is, you know, just train a smaller model. Go get a refund on half your GPU chips, and just build a small model from the beginning, without needing to train the huge teacher model first. AI engineers like to argue about which approach is better. In short: smaller models are faster but less accurate.

In fact, you can train more than one small model for less cost than a big one, which should really be called a “multi-mini-model” architecture (triple-M!). Instead, it’s called “multi-LoRA” because AI researchers like quirky names. If you’re got an iPhone with Apple Intelligence baked in, that’s the model architecture it’s using.

There are many ways to improve the arithmetic. The first trick is that someone noticed that matrix multiplication is like:

1. Multiply stuff, and
2. Add it up.

Here’s an idea: do both things together. There are now CPU and GPU hardware instructions that do exactly that, and it’s called “Fused Multiply-Add” or FMA. Hence, if your code has both a multiplication and an addition operation, then you’re behind the times.

Fuse them together!

Another way is to use smaller data. For example, there’s a fancy technique called “quantization” that really just means using smaller numbers.

The latest Blackwell GPU chips are great at “FP4” processing in all those Tensor Cores. What this means is using data that is 4-bit floating-point (FP4) instead of 32-bit floating-point (FP32) for all the numbers we’re using inside the matrix multiplications. This drop from 32-bit to 4-bit is eight times less computation, according to my calculations.

Hence, eight times faster AI engines.

Another way to make matrices smaller is to “prune” their numbers. I mean, if your model has a billion numbers, may you don’t really need all of them. Unfortunately, since AI engineers don’t really understand what all of the numbers do, we also don’t really understand what happens if we throw some away. The early research papers in the 1990s on this technique were about “Optimal Brain Damage” and it’s an inside joke that’s not really a joke.

The idea is that if a number is 0.0001, then just pretend it’s actually zero. If the weight of a signal is that small, it might as well be zero, so just throw it away. The simplest way is just to scan all the numbers through the whole model for small ones to discard, which is called “magnitude pruning.”

The other way is to look at numbers in particular parts of the model, which is called “structured pruning.” It’s like throwing away a whole lobe or a whole cortex.

There are literally four ways to prune the different model structures, along the different model dimensions:

- Length — input token pruning (i.e., throw away words)
- Depth — layer pruning (“early exit”)
- Width — attention “head” pruning (“sparse attention”)
- Model dimension — embeddings pruning (“activation sparsity”)

Any way you cut it (I mean, prune it), there’s fewer weights and less computation.

Hence, you prune and prune until there’s more zeros than non-zero numbers, and then it’s called “sparsity.” And there are so many ways to do “sparse matrix multiplications” inside a GPU that AI engineers call it terms like “sparse MatMul” or “spGEMM” or other names you can’t print.

Anyway, fast.

# Training

Inference takes milliseconds to answer a query. Training a big model can take weeks or months. There are faster GPUs and software algorithms that have sped up training since the olden days (last year), but models are getting bigger, too.

When training a big AI model, the most important thing you need is blankets. All of the AI engineers on the training team have to sleep in the data center for days or weeks. The facility is air-conditioned and liquid-cooled down as low as you can get, which isn't actually that low when you have 100,000 overclocked GPUs running. The training engineers aren't really doing much except watching the monitoring dashboard and waiting for the training phase to go: *splat!*

I'm only half kidding.

Training really does fail, and quite often, which is why you use “checkpoints” for training updates (it's a fancy word for backups). The idea is that you checkpoint often, and when it all falls over in a crying heap, then you restart from the last checkpoint. When you realize that it costs tens of millions of dollars to run training on a big cluster, you can see why it's important to have frequent backups.

Why does training fail?

Ah, yes, there are plenty of research papers on that. There are issues like vanishing gradients, exploding gradients, training instabilities due to large outliers, and all sorts of other obscure statistical reasons, which are boring, so let's skip those. More interesting reasons include:

1. Hardware bugs
2. Software bugs
3. Real bugs
4. Space bugs

Hardware bugs are surprisingly common. Well, no, actually not common, but when you have 100,000 of them, then it's not uncommon. GPUs overheat and burn out. Old GPUs are the worst, especially if you've been a cheapskate and bought used GPUs from a retired Bitcoin miner. Weirdly, brand new GPUs can fail, too, due to an occasional fault in the chip manufacturing process.

The error rate is very low, but multiply that by 100,000. Middle-aged GPUs are the sweet spot, so you ideally want to run in your new GPUs with some gentle warm-ups (like a new Porsche). Actually, training algorithms are now good enough to detect a failing GPU and isolate it, but it's not always 100% accurate, so that's when the sleeping engineers need waking up.

Software bugs are an error in the code by the C++ programmers who wrote the training software for the GPUs. Of course, that never happens, since good coders never misplace a semicolon, except for that one time with Microsoft Vista over 20 years ago. Furthermore, we can always blame the hardware engineers or the network engineers. Anyway, let's move on.

Real bugs are not very common these days. If a roach or a small lizard gets into the data center, and ends up next to a GPU, it'll get baked into the training process, literally. Thankfully, most data centers are locked-down so tight to keep out the dust that not many insects or reptiles make an impact.

Space bugs are the funniest thing! Here is where you, Dear Reader, are 100% convinced that it's a joke, and yet, it's really not.

Cosmic rays are a type of electromagnetic radiation that comes in from space. Normally, nobody notices them because they rarely interact with matter, and even if they do, it's such a minor effect that even a human body cell will ignore it and move on with life. However, GPUs have transistors that are etched into silicon at a scale of a few nanometers, which could be two, but let's say five. In comparison, a human cell is at least 10,000 and maybe 100,000 nanometers in size.

Once in a while, a GPU gets hit by a cosmic ray. And once in a while, it goes near a tiny transistor embedded in the silicon. And once in a while, it hits a transistor. And once in a while, it hits at the right time.

A bit gets toggled.

It's a very rare event. But multiply the odds by 100,000 GPUs. And then multiply again by a process that takes days or weeks.

## **Don't Forget the Network**

Programmers tend to avoid network engineers, because they're covered with dust from crawling under the raised floor to fix cables all the time. But AI engines need networking with the highest bandwidth to connect those clusters of 100,000 GPUs that do all the work.



The reason for networking depends on the phase:

- Training — send the training data out, get the weight updates back.
- Inference — send the user queries out, share some caches, get homework essays back.

Yawn! It's true that NVIDIA has a bunch of networking products like NVLink and stuff, with coverage of InfiniBand, Ethernet, BlueField, and more. However, the company only makes about \$13 billion US dollars in annual revenue from networking products, so nobody pays any attention to the networking area.

I mean, peanuts!

Pity the poor SVP of Networking at NVIDIA. They run a business bigger than over half the stock market, but never get a CNBC interview.

## The Question

Here's the real question about AI technology: is it fast enough? Short answer: No.

We're getting better at running big models at a faster clip, but these big models aren't really that great. I mean, they're amazing in some areas, but, come on, so many dumb things are still coming out of its mouth.

The whole industry is going to need a bigger model, or, more likely, a ton of much bigger models, each of them tweaked to run in particular contexts (e.g., doctors, lawyers, marketing managers, etc.). We're not close to that.

In order to fix all of the areas where AI is still faulty, we need to train it with lots more data, and make the models much bigger. Hence, here's the real question to ask:

*How much faster is needed?*

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# 16. The Sweetest Lesson

## Brains are 50 Times Bigger

Your brain is 50 times bigger than the best AI engines today. Hence, to get to an intelligence AI model, we might need 50 times more compute power. Don't believe me? Do you think ChatGPT is smarter than you?

Let's look at the facts about brains and models.

The biggest AI model is about two trillion weights. That's for GPT-4 from OpenAI, and we don't even officially know its size, but only from "leaks" we've heard that it was 1.76 trillion total weights (split into eight parts).

Is that the biggest model?

Indeed, GPT-4 was in March, 2023, so it seems likely that the state-of-the-art is more. The weight count of OpenAI's "Strawberry" reasoning model released in September 2024 has not even leaked, but we can reasonably assume it was more.

And there are a handful of other companies that are talking about making models with "trillions" of weights. Most of the details are not disclosed in research papers or press releases, but you can see the word "trillion" in patents and job ads.

It seems very likely that the latest models are above two trillion weights, but probably not by a lot, because the computation needed to run massive models is immense. You don't just train a two trillion weight model once, and done. Rather, you have two trillion weights that need to run as "inference" for every user's query after you release your model to the public.

How does your brain compare?

Firstly, it has around 86 billion neurons. There are various research papers supporting this, and it can go up to around 100 billion neurons. Even so, 86 billion neurons is substantially less than 2 trillion by a factor of about 23.

So, an AI model is 23 times bigger than your brain?

Not so fast!

We're making the wrong comparison here. It's measuring silicon apples against carbon oranges.

Weights are not neurons. No, the neuron-equivalent structure is the “model dimension” of all those neural network computations in the AI engine. A neural network is based on a matrix, like in High School math class.

The equivalent of a neuron in AI is the length of the sides of the matrices, rather than all the numbers inside the matrix. The weights in an AI model are numbers telling it how much “weight” to give to a connection between two neurons, represented in a vector of artificial neurons.

Anyway, the point is that the weights are more like “connections” between a pair of neurons. It's not a surprise that the human brain has these types of connections, because neural networks actually copied that, and made up the idea of weights being their connections.

In the brain, we call them “synapses” and they connect two neurons together via a “dendrite” physical structure.

How many synapses?

Well, the official answer is 100 trillion synapses in the human brain. This sounds like a made-up statistic, even when a chatbot tells you, so we'll stress test its assumptions below. But first, let's summarize the situation:

- AI Models — 2 trillion weights
- Human brain — 100 trillion synapses.

Like I said earlier, your brain is 50 times bigger.

## Really That Big?

It's fair to question that 100 trillion synapse statistic. Such a big, round number just sounds like made-up science. In fact, the overall method to get to that number is simplistic:

*100 billion neurons time 1,000 synapses per neuron.*

There are really two numbers to investigate here. The number of neurons is more accurately believed to be around 86 billion, so maybe that drops our estimate down by 16% overall.

On the other hand, Pakkenberg et. al. (2003) estimates 0.15 quadrillion total synapses, which is more than 50% higher than the overall 100 trillion total. Another analysis is by AI Impact (2015), based on Chudler's facts from neurology textbooks (undated), gives an even higher estimate of 1.8-3.2 times  $10^{14}$ , which is 180-320 trillion synapses.

Unfortunately, we can't be sure, because no-one has taken the time to sit down and count all those synapses. Instead, there are various estimates based on the weight and volume of different parts of the brain and the apparent density of synapse cell structures within the brain of humans and some animals.

As is obvious from the range in estimates, it's not an exact science, but this still seems to be based on reasonable assumptions.

Finally, an obvious but important point that underpins this analysis: *neurons matter*. The intelligence of humans is closely correlated to the number of neurons and the physical size of the brain. For example, Azevedo et. al. (2009) and Herculano-Houzel (2009) both show that human intelligence is based on us having a linearly scaled-up version of primate brains.

## Maybe Less

Yes, the analysis may be incorrect, and the analogy between weights and synapses is not perfect. Perhaps a lot of the 100 trillion connections are doing unimportant things that an AI engine doesn't need. The vast majority of your brain is not doing high-level reasoning.

Rather, your brain has to do a lot of other things related to its attached carbon body. There are plenty of neurons in the brainstem and other similar regions. The brainstem is around 2.6% of the human brain by weight, giving an estimate of 2.2 billion neurons out of the 86 billion total neurons. The whole autonomous nervous system has to control our breathing, heartbeat, and dozens of other systems.

*An AI won't need that.*

There's also a lot of input signal processing that can perhaps be avoided in a computerized LLM brain. For example, a lot of the brain's power is consumed by processing video inputs, and AI engines may not need to do that.

There are non-LLM ways to process video inputs, so maybe we can hook those up to an LLM. Hence, the LLM itself wouldn't need to do all of that work to process the basic video features like colors and intensities. However, the LLM still has to do the higher-level processing, such as detecting shapes and making sense of them.

## Maybe More

On the other lobe, it could be that 100 trillion synapses is an underestimate. Indeed, a number of research papers give much larger numbers. Pakkenberg et. al. (2003) gives an estimate of "0.15 quadrillion" and that's the same as 150 trillion synapses. And AI Impact's 2015 article cites to an alternative statistic of 7,000 synapses per neuron, which when combined with 86 billion neurons, would put us at about 600 trillion total synapses.

Those are some mighty big numbers about what's between your ears. To put it into context, let's divide by two (using AI):

- 100 trillion — 50 times
- 150 trillion — 75 times
- 180 trillion — 90 times
- 320 trillion — 160 times
- 600 trillion — 300 times

In comparison to the 2 trillion weights in state-of-the-art AI models, all these numbers give ratios more than 50 times greater. Indeed, 150 trillion synapses gives a ratio of 75 times higher, and the upper bound is 600 trillion synapses, with a ratio of human brains being over 300 times larger.

Which one will it be? Your guess is as good as mine. Might need some more GPU chips.

## Smart Coding

Another variable here is that the brainy boffins in the AI labs have found numerous advanced algorithms to make things go faster. For example, the GPT-4 model has 2 trillion total weights, but they're actually split up into eight separate areas, called "experts" in what's known as a Mixture-of-Experts (MoE) architecture.

Each expert in GPT4- was about 200 billion parameters. Similarly, the DeepSeek model that matched and exceeded this performance was less than 600 billion parameters, and had even smaller experts.

I'm not sure which way this cuts the analysis. If the state-of-the-art models are 200 billion rather than two trillion weights, does this mean that AI models don't need to be as big as the human brain? Maybe an AI model only needs 10 trillion total weights.

Alternatively, does this nuance mean that the AI models have ten times further to travel before they match the full intelligence of a brain?

## The Bitter Lesson Again

Whatever the answer to this analysis, it seems clear that more compute is needed. It sounds like another case of the bitter lesson, doesn't it? We just need to brute-force up another 50 times greater compute power, and then it's the same as the 100 trillion synapses in the human brain.

This level of extra computation power seems beyond our reach at the moment. However, it's not unimaginable when you consider the rate of advances in GPU chip workloads and the newer, more efficient algorithms being discovered to run the AI computations on these chips.

So much for all those reasoning algorithms!

Thus, here we are on the verge of learning the bitter lesson all over again. Instead of making advances by using intelligent and insightful new methods of thinking, we're just going to throw more electricity and C++ programmers at the problem.

# The Sweetest Lesson

Is it the bitter lesson? Sure, the idea is to brute-force a lot more GPUs in 100 trillion weight models. There's going to be plenty of computation power needed over the next few years as we advance the state-of-the-art models in both training and inference.

But the bitter lesson actually has two factors, of which brute-force hardware is only one part. Let's see if they both fit:

1. Brute-force computation, and
2. Algorithms that differ.

Can you see the mismatch? There needs to not only be brute-force computations, but also the abandonment of human-based reasoning in favor of simpler number crunching. At first, this also seems like a match, because those tricky reasoning algorithms will probably be gone. It'll just be GPUs and matrices and lots of number crunching.

But, then, inspiration.

Maybe we're not going to use a fancy reasoning algorithm on top of all those LLMs. The path to intelligence may not be a better "controller" that manages all of those low-level computations. So, the most advanced AI algorithms won't be using human-style reasoning. But, you know what, it's kind of weird, because here's the thing:

*We already are!*

There's this whole theory of neural networks that forms the basis of AI theory. For decades, it was a kind of backwater in computing research, where the results were not very impressive. Gradually, it grew in importance as the results from Machine Learning models, which is old-school AI theory, started to be used in real-world activities, like recommending which movies you should watch. Eventually, the advent of hyperscale GPUs led to the GPT series of LLMs, and the rest you already know.

Hence, this is not the bitter lesson. The whole of AI theory in the computing industry is about neural networks, which means this:

*Copying the human brain.*



It doesn't stop there at copying the basic human architecture. The AI industry is effectively copying all the workarounds and extensions that we use to make humans smarter:

- Tools — e.g., computer usage by LLMs.
- Data sources — e.g., LLMs now search the internet.
- Training — it's like sending LLMs to High School, where they read a textbook.

In summary, AI models are based on not just copying human brains, but also imitating all of the ways that humans learn. And it's not just the main neural network algorithm that's copied from a carbon brain. It's all of the workarounds, too. If we ever get to a truly "intelligent" model, and I do think it's an "if" not a "when" for the achievement of "Artificial General Intelligence" (AGI), then it's going to be achieved by copying everything we know about human intelligence.

And that's the sweetest lesson of all.

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